Maths & Calculations Guidelines

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Policy and Culture of Maths at Brettenham

Brettenham Primary School is committed to improving maths outcomes for children by focusing heavily on the concrete, pictorial, abstract (CPA) approach, alongside constant retrieval of previous knowledge and skills. A large percentage of children at Brettenham are registered as having English as an additional language, therefore, with a strong understanding of number work as a foundation, they have a better grasp of the theory of mathematics, which subsequently supports their reasoning skills.

When teaching maths, the pedagogy of the method or strategy is essential. Both the teachers and the children need to demonstrate understanding of these methods and strategies by constant articulation of the steps. Children should be constantly questioned verbally as to why they have elected to make a choice or what the next step of the method is. Children must be proficient in explaining their reasoning using key mathematical vocabulary using the sentence stems provided. Concrete resources or pictorial representation should be used alongside modelling methods to support all our learners and create an inclusive environment for all.

Implementation of the Policy

Each teacher has a commitment to moving children on to the next level as and when they are ready. We have to foster a culture of having high expectations, pushing each child to achieving their full potential. Consistency in approach throughout the school is the key to success.

How Stages Develop

The methods in this document rely on each other to a degree, and also place a great emphasis on the children understanding place value. As children move from one stage to another, the focus moves from:

1) Concrete understanding using manipulatives
2) Pictorial representations of concepts where appropriate
3) Abstract written methods
4) Speed, fluency and efficiency

All stages of the calculation policy should work alongside the development of reasoning skills and articulation of understanding. Pupils should be using mathematical language when using calculations to solve problems, make generalizations, find patterns and explain their ideas. Once a child has fully understood the concept taught, they should move on to mastery challenges (justify, prove, investigate questions), enabling them to develop a deep knowledge of mathematics.

Fluency

At Brettenham, we have found that constant retrieval is the key to success. If children do not regularly use a skill, they lose it. Therefore, every lesson begins with a starter question which recaps previously learnt skills. This is also useful for AfL, as it enables teachers to quickly identify any areas of mathematics which may need to be revisited. KS1 have 3 fluency lessons a week which focus on mastering number in order to set strong foundations for KS2 who will continue to retrieve previous knowledge at the start of every lesson. In KS2 , every Friday has a fluency focus on times tables and learning from the week or where teachers have identified gaps.

Lesson Expectation

KS1:

The expectation for KS1 is that classes have 5 maths lessons timetabled a week for curriculum lessons. There are also an additional three 15 – 20 minute sessions a week focusing on fluency and mastering number.

KS2:

The expectation for KS2 is that classes have 5 maths lessons timetabled a week. Lessons 1 – 4 focus on teaching the maths curriculum objectives. The final lesson is used to develop fluency focusing on times tables and gaps in children's knowledge.

<table>
<tr>
<td>Monday
Tuesday
Wednesday
Thursday</td>
<td>
5 mins for children to answer
Reveal answers
Retrieval – Questions based on previous learning: methods or fluency practice.
A few minutes (to go over new words for this lesson)
DVD – Explicitly teach appropriate vocabulary for the lesson. Children say the word. Provide definitions. This may change throughout the week based on what you are teaching.
5/10 minutes
FLUENCY:

I do – Live modelling, teacher uses teacher talk to model their thinking. This will be mostly based around fluency at this point. You can model with manipulatives, flipchart, under the visualiser etc. Stick to one method at a time – e.g. bar models, part whole models etc.

At this point, you would also share steps to success or success criteria with the children alongside your modelling.
Check for understanding – Do you need to remodel or are they ready for a turn themselves?

5/10 minutes
We do – Provide children with examples (like you modelled) using different numbers. You may provide partially worked examples or one where a mistake has been made and they need to correct it.
AFL –
10 minutes
You do – Children who are ready can go and start their fluency in their books.
Some children may need to stay with you for more modelling or scaffolds to support their learning.
Don't give too many questions (5 or 6) for them to demonstrate their fluency and varied fluency. You can still direct children to the questions you would like them to start with.

REASONING AND PROBLEM SOLVING:
Bring children back together to model the challenge question - at this point, some of the class may still be working on their fluency.

Repeat I do, we do you do for challenge question.
The we do and you do should mirror the question you modelled with but have different numbers.

Children who are ready can have a go at the problem solving question.
</td>
</tr>
<tr>
<td>Friday</td>
<td>
Maths Challenge lesson

Maths Challenge – targeted questions based on what has been taught so far. Focus on developing fluency based on teacher assessment gap analysis. You can use the White Rose fluency example questions.

During this time, if you have any children who constantly underperform. Work with them to remodel/reteach a concept. Then when other children are going through the answers, they can have a go at one or two questions based on the work you did with them.

Reveal answers – any gaps can be addressed at the start of the following week's Friday lesson or be revisited during retrieval starters the following week.
</td>
</tr>
</table>

	Times tables – TTRS sound check or garage heat map. Track scores and send to Alex. Reasoning or problem solving / addressing misconceptions The rest of the session can be used to explicitly teach reasoning and problem solving based on the skills you used in maths throughout the week. Alternatively, if you feel that there are still gaps in learning by the end of the week, you can revisit these. Plan one quality reasoning or problem solving question for the Friday in the style I do, we do, you.

Number formation:

0 1 2 3 4 5 6 7 8 9

Use commas when presenting numbers over 1,000:

2,573 34,004 148,372 1,276,301

Working Walls:

Every classroom should have working walls which reflect the current learning taking place in the class. The working walls should include:

Key vocabulary

Sentence stems

Worked examples

The representations that you have used (these could be concrete or pictorial)

Counting

EYFS

Practical Maths

Nursery

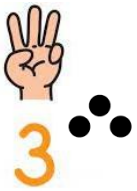
- Take part in finger rhymes with numbers.
- Combine objects like stacking blocks and cups. Put objects inside others and take them out again.



- React to changes of amount in a group of up to three items.
- Compare amounts, saying 'lots', 'more' or 'same'.
- Develop counting-like behaviour, such as making sounds, pointing or saying some numbers in sequence.
- Count in everyday contexts



- Develop fast recognition of up to 3 objects, without having to count them individually (subitising)



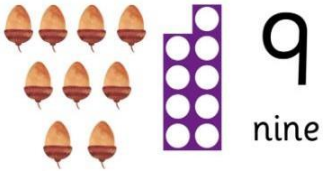
- Recite numbers past 5
- Say one number for each item in order: 1,2,3,4,5
- Know that the last number reached when counting a small set of objects tell you how many there are in total



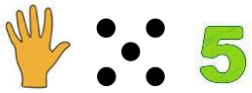
- Show 'finger numbers' up to 5
- Link numerals and amounts showing the right number of objects to match the numeral up to 5.
- Experiment with own symbols and marks as well as numerals
- Solve real world maths problems with numbers up to 5
- Compare quantities 'more than' and 'less than'

Reception

- Count objects, actions and sounds
- Subitise numbers up to 5
- Link the number symbol with its cardinal number value



- Count beyond ten
- Compare numbers
- Explore the composition of numbers to 10
- Verbally count beyond 20, recognising the pattern of the counting system
- Explore and represent patterns within numbers to 10, including evens and odds, double facts and how quantities can be distributed equally.



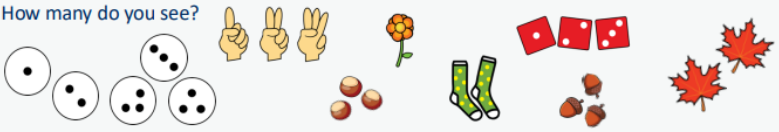
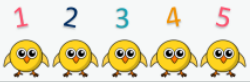
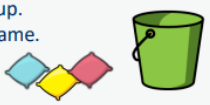
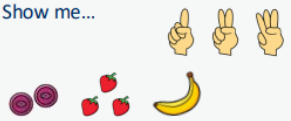


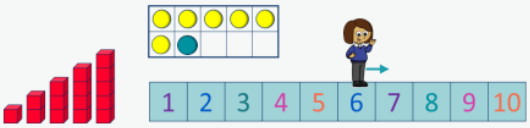
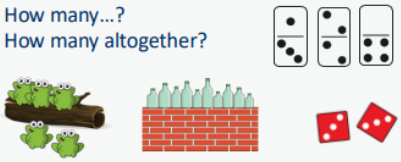
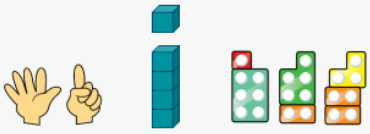
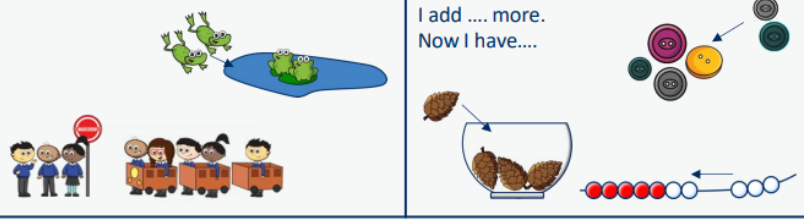
Addition

Year group	Skill
Nursery	• Subitise to 3 • Count how many • Make numbers to 5 • Add 1 more (through songs and rhymes)
Reception	• Conceptually subitise to 5 • 1 more • Notice the composition of numbers within 10 • Combine 2 groups • Add more
Year 1	• Add together • Add more • Bonds within 10 • Related facts within 20 • Missing numbers
Year 2	• Add 1s to any number (related facts) • Add three 1-digit numbers • Add across a 10 • Add multiples of 10 • Add 10s to any number • Add two 2-digit numbers (not across a ten) • Add two 2-digit numbers (across a ten) • Missing numbers
Year 3	• Add 1s, 10s and 100s to a 3-digit number • Add two numbers (no exchange) • Add two numbers across a 10 or 100 • Complements to 100 • Add fractions with the same denominator within 1 whole
Year 4	• Add 1s, 10s and 100s to a 4-digit number • Add up to two 4-digit numbers • Add decimal numbers in the context of money • Add fractions and mixed numbers with the same denominator beyond 1 whole
Year 5	• Add using mental strategies • Add whole numbers with more than 4 digits • Add decimals with up to 2 decimal places • Complements to 1 • Add fractions with denominators that are a multiple of one another
Year 6	• Add integers up to 10 million • Add decimals with up to 3 decimal places • Order of operations • Negative numbers • Add fractions

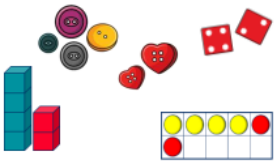
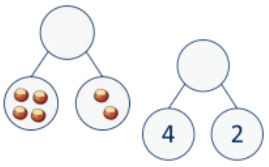
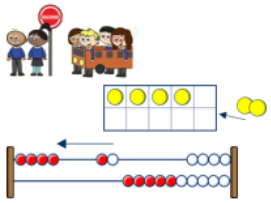
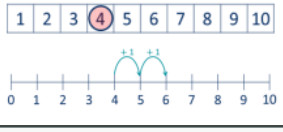
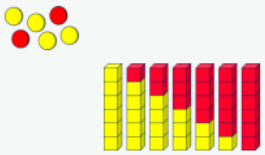
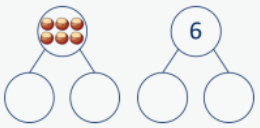
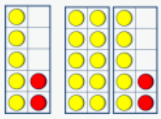
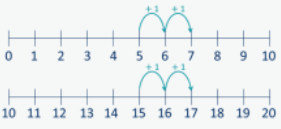
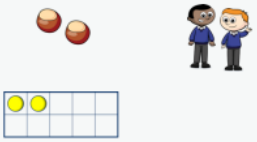
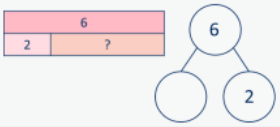
EYFS

Practical Maths

Nursery	• Begin to have an understanding of numbers to 5 • We recommend focusing on noticing and representing small quantities, perceptual subitising and counting.
Progression of skills	**Key representations**
Subitise to 3 Instantly see how many.	How many do you see? 
Count how many Begin to count objects using 1-1 correspondence.	How many are there? 1 2 3 4 5  Count out … from a larger group. E.g. Collect 3 beanbags for a game. 
Make numbers to 5 Start by showing 1, 2 and 3 using fingers.	Show me…  Begin to link numerals to quantities. 
Add 1 more Through stories, songs and rhymes.	How many do I have now? 

Reception	• Have a deep understanding of numbers to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts.
Progression of skills	**Key representations**
Conceptually subitise to 5 Notice the parts that make up the whole.	What do you see? How do you see it? 
1 more Continue to link to stories, songs and rhymes.	1 more than … is … 
Notice the composition of numbers within 10 Link to stories, songs and rhymes.	How many…? How many…? How many altogether?  How many ways can you make…? 
Combine 2 groups 2 groups are combined to find the total.	There are …. There are …. There are …. altogether.  …. and …. make …. 
Add more A quantity is increased.	First… Then…. Now…. I have …. I add …. more. Now I have…. 

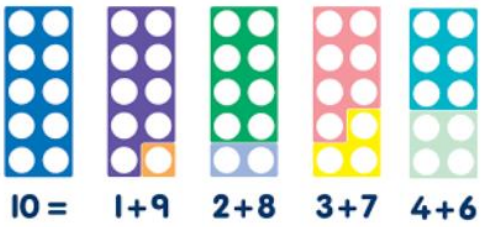
Year 1

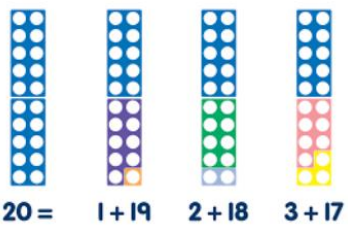
Year 1	• Read, write and interpret mathematical statements involving addition (+) and equals (=) signs. • Represent and use number bonds within 20 • Add 1-digit and 2-digit numbers to 20, including zero. • Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as 7 = □ + 2		
Progression of skills	**Key representations**		
Add together (aggregation) 2 quantities are combined to find the total.	There are ... There are ... There are ... altogether. 	... is a part. ... is a part. ... is the whole. 	... plus ... is equal to ... ... is equal to .... + ... 4 + 2 = 6 2 + 4 = 6 6 = 4 + 2 6 = 2 + 4
Add more (augmentation) A quantity is increased.	First... Then... Now... 	I start at ... I jump on ... I land on ... 	... plus ... is equal to ... is equal to ... + ... 4 + 2 = 6 2 + 4 = 6 6 = 4 + 2 6 = 2 + 4
Bonds within 10 Include bonds for each number within 10 Encourage children to notice patterns.	... is made of ... and ... ... and ... make ... 	... can be partitioned into ... and ... 	... plus ... is equal to ... 6 + 0 = 6 5 + 1 = 6 4 + 2 = 6 3 + 3 = 6 2 + 4 = 6 1 + 5 = 6 0 + 6 = 6
Related facts within 20 Make links to known facts.	I know that ... and ... = ... so ... and ... = ... 	... more than ... is ... so ... more than ... is ... 	What patterns do you notice? 5 + 2 = 7 15 + 2 = 17 7 = 5 + 2 17 = 15 + 2
Missing numbers Make links to known facts.	How many more do you need to make ...? 	If ... is the whole and ... is a part, the other part must be... 	... plus ... is equal to ... 2 + □ = 6 6 = 2 + □ 

Number Bonds:

Use of manipulatives such as Numicon to represent and show an understanding of number bonds to 10 & 20.

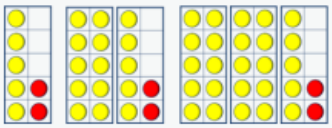
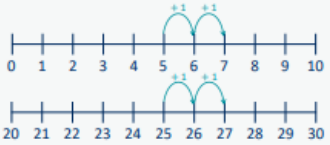
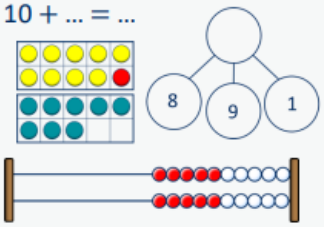
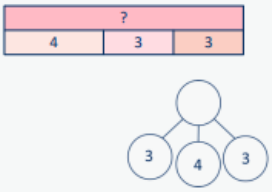
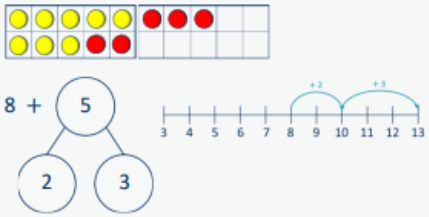
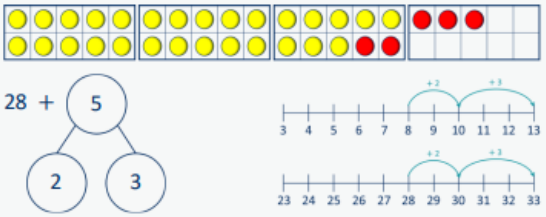
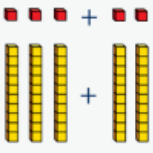
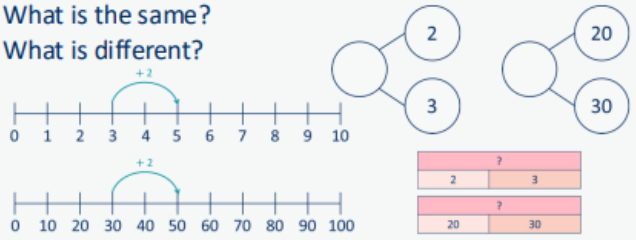
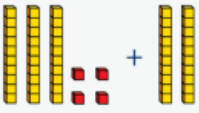
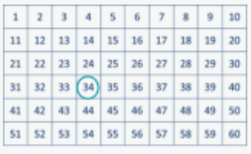
Once children are secure using manipulatives, the next step is to recall number bonds mentally.





Year 2

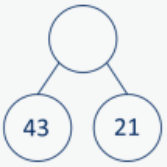
Year 2	• Recall and use addition facts to 20 fluently, and derive and use related facts up to 100
	• Add numbers using concrete objects, pictorial representations, and mentally, including:
	  • a two-digit number and 1s
	  • a two-digit number and 10s
	  • 2 two-digit numbers
	  • adding 3 one-digit numbers
	• Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.

Progression of skills	Key representations		
Add ones to any number (related facts) Make links to known facts.	I know that … and … = … so … and … = … 	… more than … is … so … more than … is …  	What do you notice? Can you continue the pattern? 5 + 2 = 7 15 + 2 = 17 25 + 2 = 27…
Add three 1-digit numbers Prompt children to understand that addition can be done in any order and to make links to known facts.	… and … are a bond to 10 10 + … = …  	Double … + … = …  	What do you notice? Which addition is the easiest to calculate? 8 + 9 + 1 = 8 + 1 + 9 = 9 + 1 + 8 =
Add across a 10 Partition the number being added to make a full ten.	… can be partitioned into … and …  	I add … to get to … then I add … 8 + 5 = 13 28 + 5 = 33  	
Add multiples of 10 Make links to known facts within ten.	… ones + … ones = … ones so … tens + … tens = … tens  3 + 2 = 5 30 + 20 = 50	What is the same? What is different?  	
Add 10s to any number Make links to known facts.	… tens + … tens = … tens … tens and … ones = … 	To add … I need to add 10 … times. 	I know that … and … = … so … and … = … 30 + 20 = 50 34 + 20 = 54

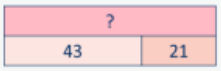
<table>
<tr>
<td>Add 2-digit numbers
(not across a ten)

Lining up ones and tens in columns will support with later written methods.</td>
<td>... ones + ... ones = ... ones
... tens + ... tens = ... tens



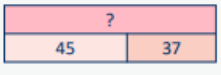
3 ones + 1 one = 4 ones
4 tens + 2 tens = 6 tens
6 tens + 4 ones = 64

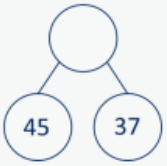
 
</td>
</tr>
<tr>
<td>Add 2-digit numbers
(across a ten)

Begin to exchange 10 ones for 1 ten.</td>
<td>There are .... ones, so I do/do not need to make an exchange.

... ones = ... ten and ... ones

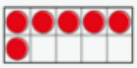
 

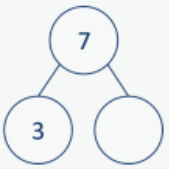


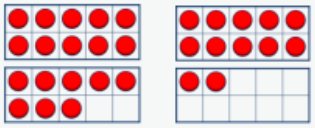


5 ones + 7 ones = 12 ones
12 ones = 1 ten and 2 ones
4 tens + 3 tens + 1 ten = 8 tens
8 tens and 2 ones = 82</td>
</tr>
<tr>
<td>Missing numbers

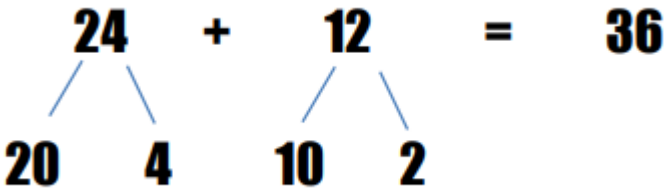
Solve missing number problems and use the inverse to check.</td>
<td>How many more do you need to make ...?

 
6 + □ = 10
10 − □ = 6</td>
<td>If ... is a whole and ... is a part, then ... is the other part.

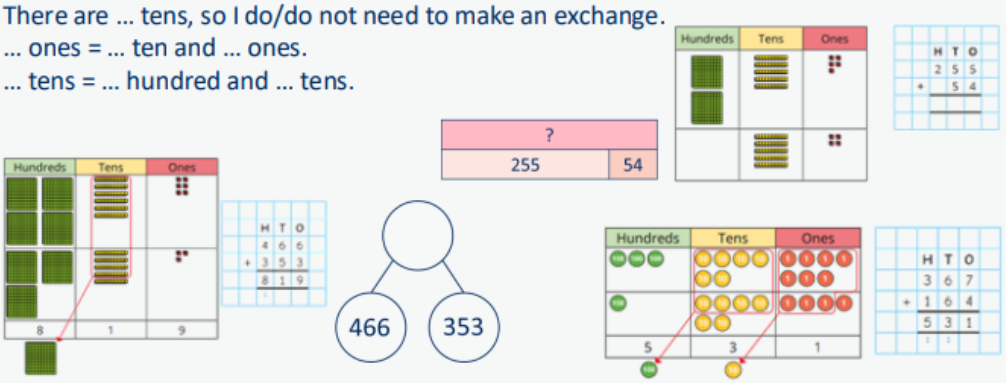
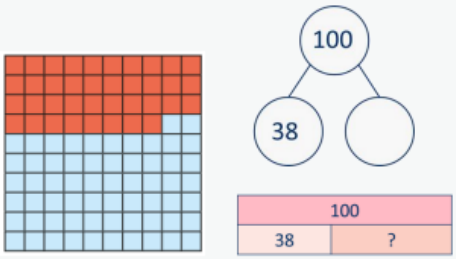
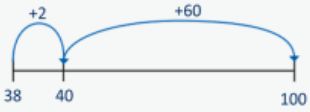
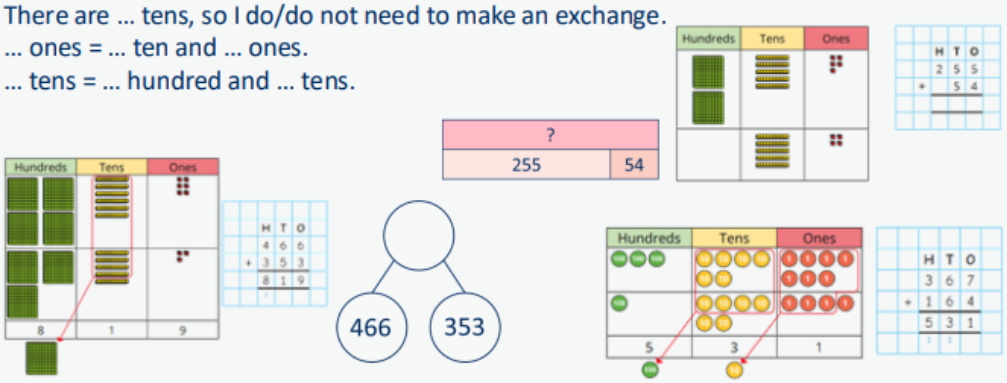
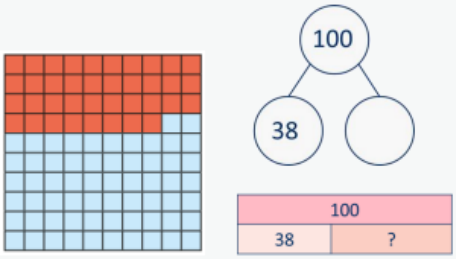
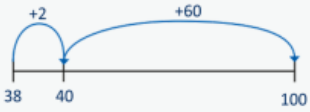
□ + 3 = 7
7 − 3 = □
 
</td>
<td>... can be partitioned into ... and ...

10 + 8 = 12 + □
  </td>
</tr>
</table>

Partitioning to add 2 two digit numbers.

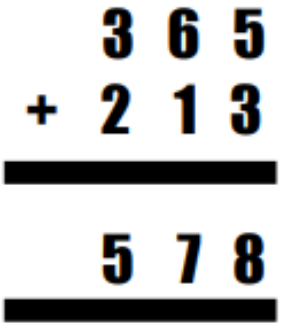


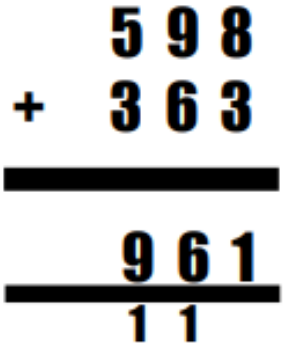
Year 3

Progression of skills	Key representations
Add two numbers across a 10 or 100 Formal written method involving up to 2 exchanges including 3-digit plus 2-digit numbers.	There are … ones, so I do/do not need to make an exchange. There are … tens, so I do/do not need to make an exchange. … ones = … ten and … ones. … tens = … hundred and … tens. 
Complements to 100 Pairs of numbers which total 100	… plus … is equal to 100  I add … to get to the next 10, then … to get to 100  $38 + 62 = 100$ $62 + 38 = 100$ $100 = 38 + 62$ $100 = 62 + 38$
Add two numbers across a 10 or 100 Formal written method involving up to 2 exchanges including 3-digit plus 2-digit numbers.	There are … ones, so I do/do not need to make an exchange. There are … tens, so I do/do not need to make an exchange. … ones = … ten and … ones. … tens = … hundred and … tens. 
Complements to 100 Pairs of numbers which total 100	… plus … is equal to 100  I add … to get to the next 10, then … to get to 100  $38 + 62 = 100$ $62 + 38 = 100$ $100 = 38 + 62$ $100 = 62 + 38$

Formal methods:

Adding numbers with up to three digits using the column method. Children should be confident using column method without exchanging first.

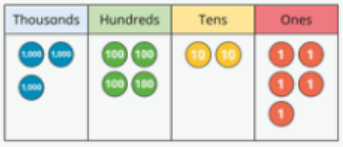
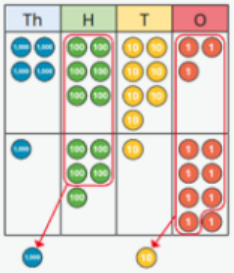
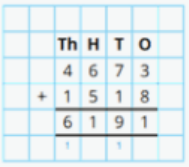




Don't forget, if you must exchange ten ones for one ten, carry the digit below the correct column.

You should show the formal written method alongside the concrete or pictorial representation.

Year 4

Year 4	• Add numbers with up to 4 digits using a formal written method. • Solve simple measure and money problems involving fractions and decimals to 2 decimal places. • Add fractions with the same denominator.
Progression of skills	**Key representations**
Add 1s, 10s and 100s to a 4-digit number Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.	The ones/tens/hundreds/thousands column will increase by …  3,425 + 3 = 3,425 + 30 = 3,425 + 300 = 3,425 + 3,000 = What patterns do you notice? 2,350 + 3 = 2,350 + 30 = 2,350 + 300 = 2,350 + 3,000 = 6,040 + 200 = 6,040 + 500 = 6,040 + 900 = 2,211 + ☐ = 2,251 2,211 + ☐ = 2,215 2,211 + ☐ = 2,511
Add up to two 4-digit numbers Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.	There are … ones/tens/hundreds so I do/do not need to make an exchange. I can exchange 10 … for 1 …  

Formal methods:

Adding numbers with up to four digits using the column method (see Year 3 strategies and consolidate understanding of the column method):

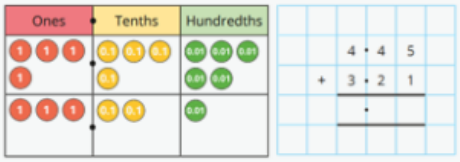
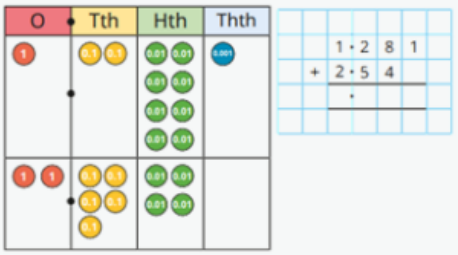
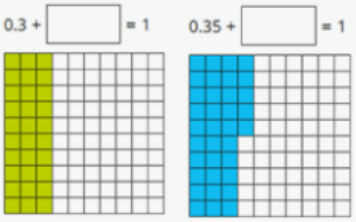
$$\begin{array}{r} 5\,9\,8\,2 \\ +\ 2\,9\,4\,6 \\ \hline 8\,9\,2\,8 \\ \hline 1\,1 \end{array}$$

$$\begin{array}{r} \square\,9\,8 \\ +\ 3\,\square\,7 \\ \hline 7\,4\,5 \\ \hline \square\,\square \end{array}$$

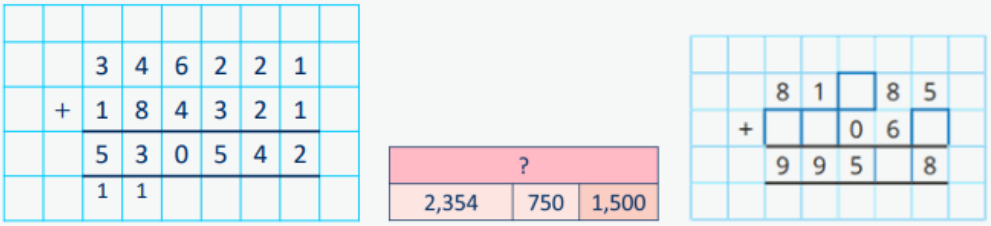
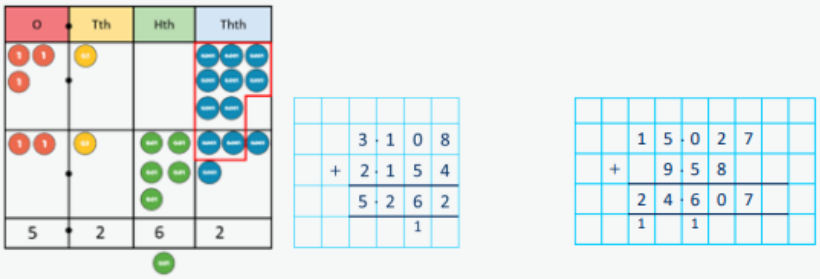
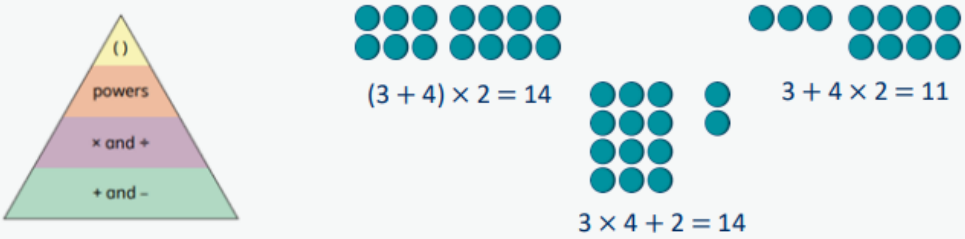
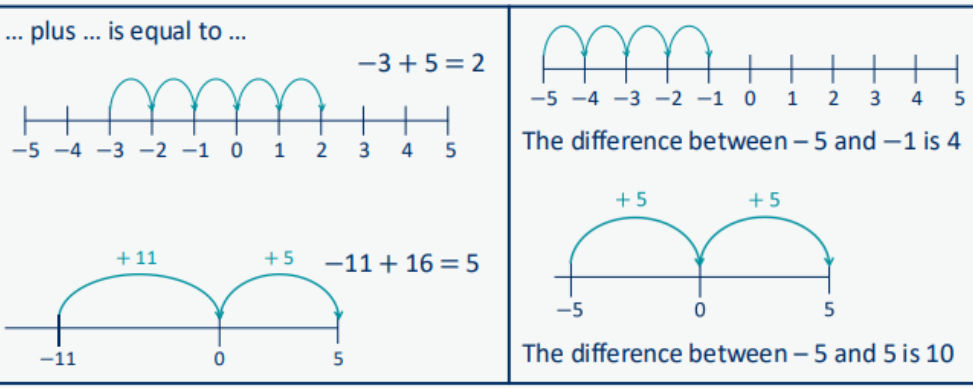
Check for understanding through missing numbers

Add decimal numbers in the context of money Emphasis on partitioning and use of number lines rather than formal written calculations.	… pence + … pence = … pence … pounds + … pounds = … pounds  45p + 25p = 70p £2 + £3 = £5 £5 + 70p = £5.70	£3.25 can be partitioned into £3 + 20p + 5p 

Year 5

Progression of skills	Key representations
Add decimals with up to 2 decimal places Progress from the same number of decimal places to a different number of decimal places, and from no exchange to exchange.	I do/do not need to make an exchange because … I can exchange 10 … for 1 …  
Complements to 1 Pairs of numbers with up to 3 decimal places which total 1 Encourage children to make links with bonds to 10 and complements to 100 and 1,000	   4 + 6 = 10 44 + 56 = 100 444 + 556 = 1,000 0.4 + 0.6 = 1 0.44 + 0.56 = 1 0.444 + 0.556 = 1

Year 6

Year 6	• Add larger numbers, using the formal written method of columnar addition. • Use their knowledge of the order of operations to carry out calculations involving the 4 operations. • Calculate intervals across zero. • Add fractions with different denominators and mixed numbers, using the concept of equivalent fractions.
Progression of skills	**Key representations**
Add integers up to 10 million Encourage children to estimate and use inverse operations to check answers to calculations.	
Add decimals with up to 3 decimal places Progress to numbers with digits in different place value columns. Encourage children to check that they have lined up the columns correctly.	I do/do not need to make an exchange because ... 
Order of operations Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction. *When no brackets are shown and the operations have the same priority, work left to right.	... has greater priority than ..., so the first part of the calculation I need to do is ... 
Negative numbers Children add to negative numbers and carry out calculations which cross 0	... plus ... is equal to ... 

Ensure that children understand that the decimal point does not move.

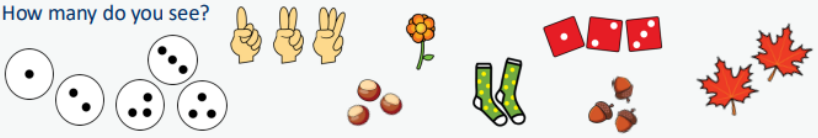
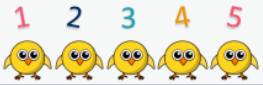
$$\begin{array}{r} 998.2 \\ +\ 275.7 \\ \hline 1183.9 \\ \hline 11 \end{array}$$

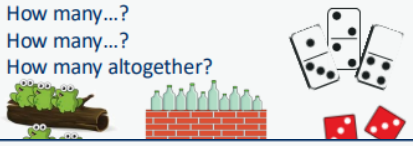
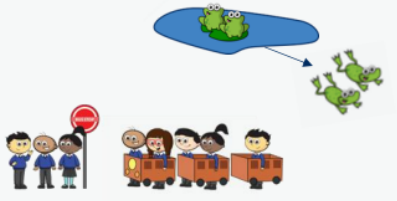
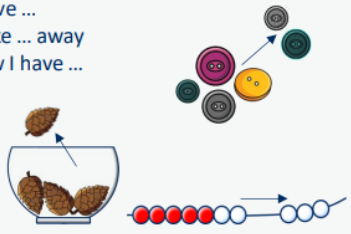
Subtraction

Year group	Skill
Nursery	• Subitise to 3 • Count how many • Make numbers to 5 • Take 1 away (through songs and rhymes)
Reception	• Conceptually subitise to 5 • 1 less • Notice the composition of numbers within 10 • Partition • Take away
Year 1	• Find a part • Take away • Bonds within 10 • Related facts within 20 • Missing numbers
Year 2	• Subtract 1s from any number (related facts) • Subtract across a 10 • Subtract multiples of 10 • Subtract 10s from any number • Subtract two 2-digit numbers (not across a ten) • Subtract two 2-digit numbers (across a ten) • Missing numbers
Year 3	• Subtract 1s, 10s and 100s from a 3-digit number • Subtract two numbers (no exchange) • Subtract two numbers across a 10 or 100 • Complements to 100 • Subtract fractions with the same denominator within 1 whole
Year 4	• Subtract 1s, 10s, 100s and 1,000s from a 4-digit number • Subtract up to two 4-digit numbers • Subtract decimal numbers in the context of money • Subtract fractions and mixed numbers with the same denominator
Year 5	• Subtract whole numbers with more than 4 digits • Subtract using mental strategies • Subtract decimals with up to 2 decimal places • Complements to 1 • Subtract fractions with denominators that are a multiple of one another
Year 6	• Subtract integers up to 10 million • Subtract decimals with up to 3 decimal places • Order of operations • Negative numbers • Subtract fractions

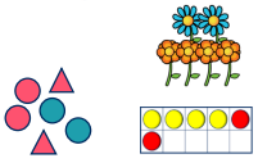
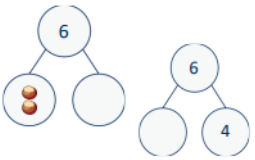
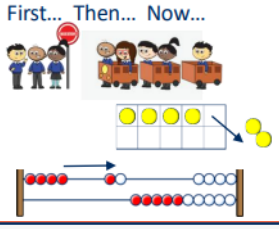
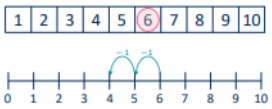
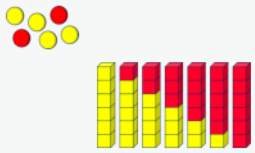
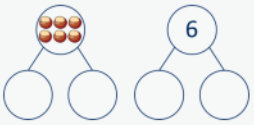
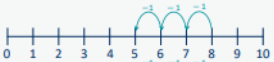
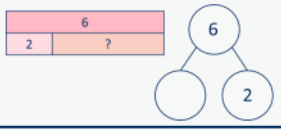
EYFS

Practical Maths

Nursery	• Begin to have an understanding of numbers to 5 • We recommend focusing on noticing and representing small quantities, perceptual subitising and counting.
Progression of skills	**Key representations**
Subitise to 3 Instantly see how many.	How many do you see? 
Count how many Begin to count objects using 1-1 correspondence.	How many are there?  Count out … from a larger group. E.g. Collect a cup for everyone at the table. 
Make numbers to 5 Start by showing 1, 2 and 3 using fingers.	Show me…  Begin to link numerals to quantities. 
Take 1 away Through stories, songs and rhymes.	How many do we have now? 

Reception	• Have a deep understanding of number to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (and some subtraction facts) and some number bonds to 10, including double facts.
Progression of skills	**Key representations**
Conceptually subitise to 5 Notice the parts that make up the whole.	What do you see? How do you see it? 
1 less Continue to link to stories, songs and rhymes.	1 less than … is … 
Notice the composition of numbers within 10 Link to stories, songs and rhymes.	How many…? How many…? How many altogether?  How many ways can you make…? 
Partition Using objects, explore different ways to partition a number into 2 or more parts.	There are … altogether. I can see … here and … there.  … and … make … 
Take away A quantity is reduced.	First… Then… Now…  I have … I take … away Now I have … 

Year 1

Year 1	• Read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs. • Represent and use number bonds and related subtraction facts within 20 • Subtract one-digit and two-digit numbers to 20, including zero. • Solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = □ – 9		
Progression of skills	**Key representations**		
Find a part Link to number bonds and known facts. E.g. 2 + 4 = 6 so if 6 is the whole and 4 is a part, the other part must be 2	There are ... in total. ... are ... How many are **not** ...? 	... is the whole. ... is a part. ... is a part. 	... subtract ... is equal to ... ... is equal to ... – ... 6 – 2 = 4 6 – 4 = 2 4 = 6 – 2 2 = 6 – 4
Take away A quantity is decreased.	First... Then... Now... 	I start at ... I jump back ... I land on ...  	... minus ... is equal to ... ... is equal to ... – ... 6 – 2 = 4 6 – 4 = 2 4 = 6 – 2 2 = 6 – 4
Bonds within 10 Focus on subtraction facts. Encourage children to notice patterns.	... is made of ... and ... ... and ... make ... 	... can be partitioned into ... and ... 	... minus ... is equal to ... 6 – 0 = 6 6 – 1 = 5 6 – 2 = 4 6 – 3 = 3 6 – 4 = 2 6 – 5 = 1 6 – 6 = 0
Related facts within 20 Make links to known facts.	I know that ... minus ... = ... so ... minus ... = ... 	... less than ... is ... so ... less than ... is ...  	What patterns do you notice? 8 – 3 = 5 18 – 3 = 15 5 = 8 – 3 15 = 18 – 3
Missing numbers Make links to known facts.	How many do you need to subtract to make ...?  	If ... is the whole and ... is a part, the other part must be... 	... minus ... is equal to ... 6 – □ = 2 2 = 6 – □ 

Use a range of manipulatives to physically take away groups of objects up to 20 (Fingers, multi-link, dienes, etc.)

- To count back from a given number using the bigger number first and subtracting the smaller number (children to have a secure knowledge of ordering numbers which will allow them to select the bigger number):

9 – 4 = 5



- Rather than using bigger numbers once pupils show a secure understanding, move on to subtraction with missing numbers:

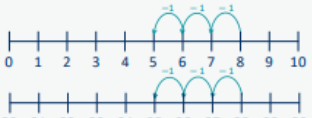
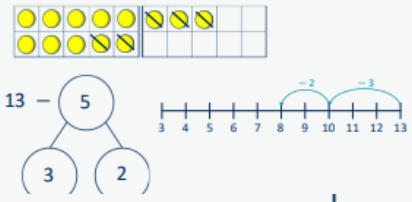
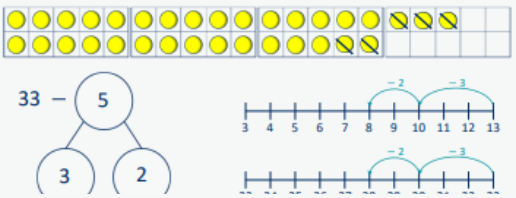
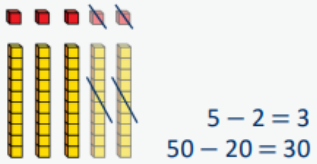
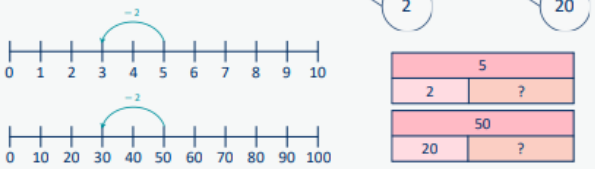
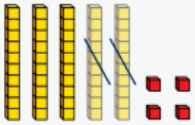
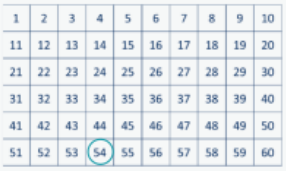
5 - 2 = □	□ = 5 - 2
5 - □ = 3	3 = □ - 2
□ - 2 = 3	3 = 5 - □
□ - □ = 3	3 = □ - □

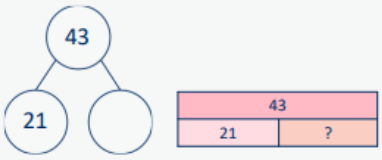
N.B. Numicon should **only** be used for difference questions and by laying the smaller number on top of the bigger number:

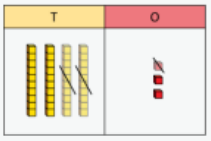


Year 2

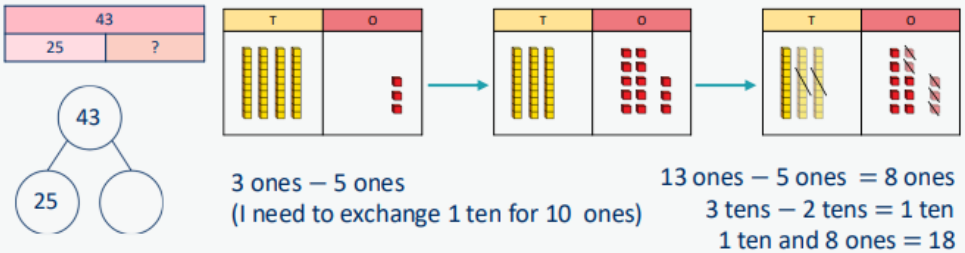
	• Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100
	• Subtract numbers using concrete objects, pictorial representations, and mentally, including:
	  • a two-digit number and 1s
	  • a two-digit number and 10s
	  • 2 two-digit numbers
	• Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.

Progression of skills	**Key representations**
Subtract ones from any number (related facts) Make links to known facts.	I know that … minus … = … so … minus … = …  … less than … is … so … less than … is …  What do you notice? Can you continue the pattern? $8 - 3 = 5$ $18 - 3 = 15$ $28 - 3 = 25$…
Subtract across a 10 Partition the number being subtracted to bridge through a ten.	… can be partitioned into … and …  Make links with related facts. 
Subtract multiples of 10 Make links to known facts within ten.	… ones − … ones = … ones so … tens − … tens = … tens  $5 - 2 = 3$ $50 - 20 = 30$ What is the same? What is different? 
Subtract 10s from any number Make links to known facts.	… tens − … tens = … tens … tens and … ones = …  To subtract … I need to subtract 10 … times.  I know that … minus … = … so … minus … = … $50 - 20 = 30$ $54 - 20 = 34$

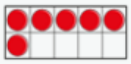
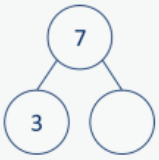
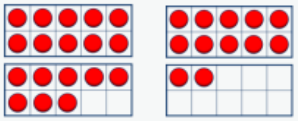
<table>
<tr>
<td>Subtract two 2-digit numbers
(not across a ten)</td>
<td>... ones − ... ones = ... ones
... tens − ... tens = ... tens
 



3 ones − 1 one = 2 ones
4 tens − 2 tens = 2 tens
2 tens and 2 ones = 22</td>
</tr>
<tr>
<td>Subtract two 2-digit numbers
(across a ten)

Begin to exchange 1 ten for 10 ones.</td>
<td>I need to make an exchange because I do not have enough ones to subtract ... ones.
 

3 ones − 5 ones
(I need to exchange 1 ten for 10 ones)
13 ones − 5 ones = 8 ones
3 tens − 2 tens = 1 ten
1 ten and 8 ones = 18</td>
</tr>
<tr>
<td>Missing numbers

Solve missing number problems and use the inverse to check.</td>
<td>How many do you need to subtract to make ...?
 
10 − □ = 6
6 + □ = 10</td>
<td>If ... is a whole and ... is a part, then ... is the other part.
7 − 3 = □
□ + 3 = 7
 
</td>
<td>... can be partitioned into ... and ...
18 − □ = 12 + 2
  </td>
</tr>
</table>

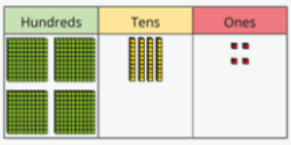
Year 3

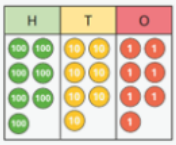
Year 3	• Subtract numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds. • Subtract numbers with up to three digits, using formal written methods. • Subtract fractions with the same denominator within 1 whole.
Progression of skills	**Key representations**

Subtract 1s, 10s and 100s from a 3-digit number

Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.

The ones/tens/hundreds column will decrease by …





444 − 2 =
444 − 20 =
444 − 200 =

777 − 4 =
777 − 40 =
777 − 400 =

What patterns do you notice?

235 − 3 =
235 − 30 =
235 − 300 =

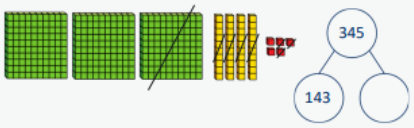
624 − 20 =
654 − 50 =
694 − 90 =

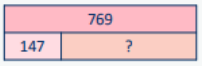
118 − ☐ = 111
181 − ☐ = 111
811 − ☐ = 111

Subtract two numbers (no exchange)

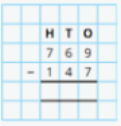
Mental strategies and introduction of formal written method.

… ones − … ones = … ones
… tens − … tens = … tens
… hundreds − … hundreds = … hundreds





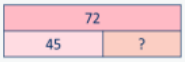


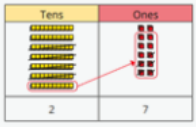


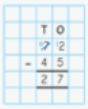
Subtract two numbers across a 10 or 100

Formal written method involving up to 2 exchanges including 3-digit subtract 2-digit numbers.

I need to subtract … ones. I do/do not need to make an exchange.
I need to subtract … tens. I do/do not need to make an exchange.
I can exchange 1 … for 10 …

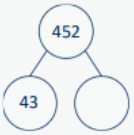




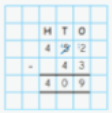










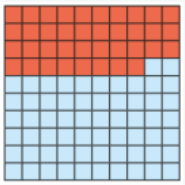


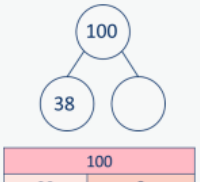
Complements to 100

Focus on subtraction facts.

Encourage children to notice patterns.

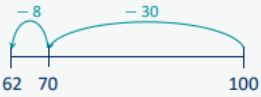
100 minus … is equal to …





I subtract … tens, then I subtract … ones.

100 − 38 = 62
100 − 62 = 38
62 = 100 − 38
38 = 100 − 62



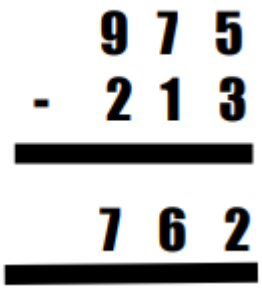
Begin with number lines:

57 - 26 = 31



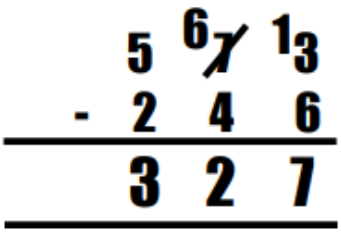
Formal methods:

Subtract numbers with up to three digits using column method.



No exchanging first.

Introduce exchanging once secure with column subtraction.



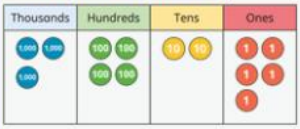
Year 4

Year 4	• Subtract numbers with up to 4 digits using a formal written method. • Solve simple measure and money problems involving fractions and decimals to 2 decimal places. • Subtract fractions with the same denominator.
Progression of skills	**Key representations**

Subtract 1s, 10s, 100s and 1,000s from a 4-digit number

Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.

The ones/tens/hundreds/thousands column will decrease by ...



3,425 – 2 =
3,425 – 20 =
3,425 – 200 =
3,425 – 2,000 =

What patterns do you notice?

4,356 – 3 =
4,356 – 30 =
4,356 – 300 =
4,356 – 3,000 =

6,940 – 200 =
6,940 – 300 =
6,940 – 400 =

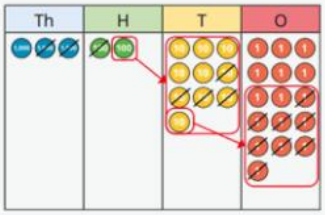
4,433 – ☐ = 4,430
4,433 – ☐ = 4,033
4,433 – ☐ = 4,403

Subtract up to two 4-digit numbers

Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.

I need to subtract... ones/tens/hundreds. I do/do not need to make an exchange.

I can exchange 1... for 10...



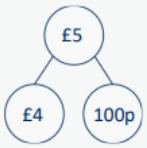


Subtract decimal numbers in the context of money

Emphasis here is on partitioning and use of number lines rather than formal written calculations.

I can partition £... into £... and 100p
£... – £... = £...
100p – ...p = ...p

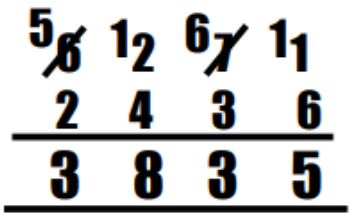
£5 – £3.26
£4 – £3 = £1
100p – 26p = 74p
£5 - £3.26 = £1.74



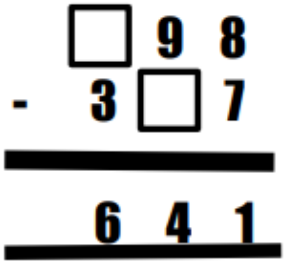
£3.26 can be partitioned into £3 + 20p + 6p



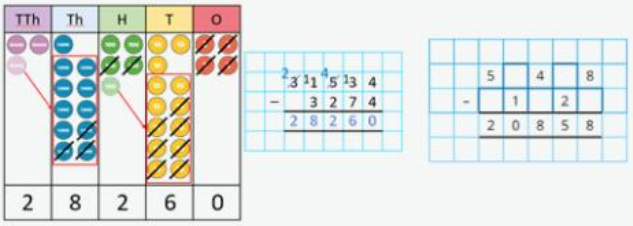
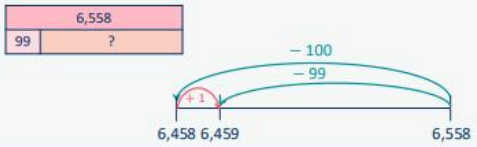
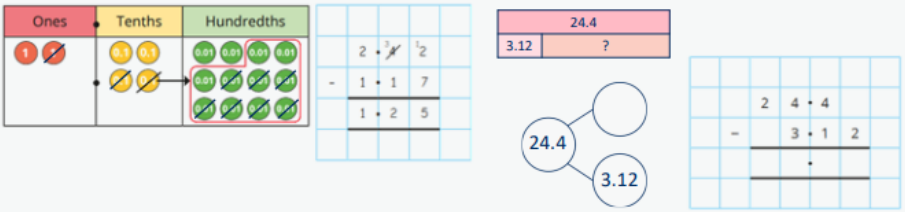
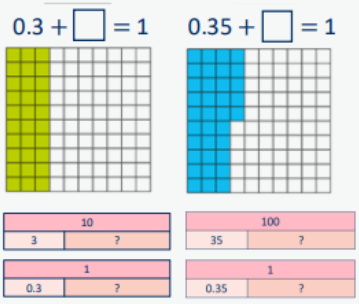
Subtract numbers with up to four-digits using column subtraction (see Year 3 strategies and consolidate understanding of the column subtraction):



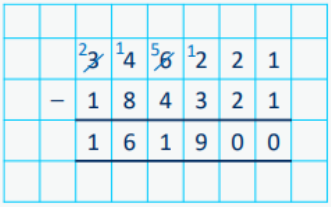
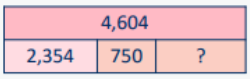
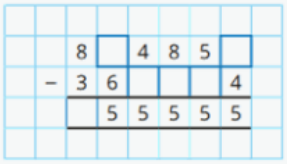
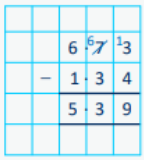
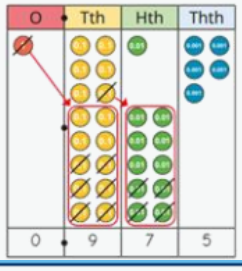
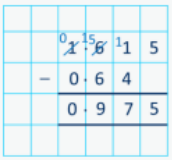
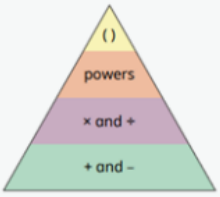
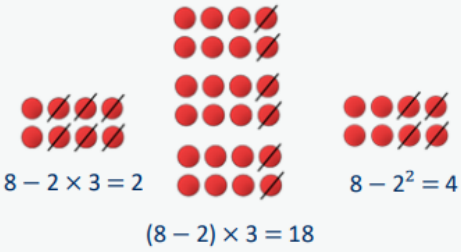
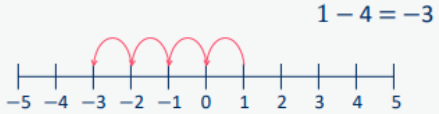
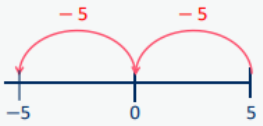
Check understanding of column subtraction through missing numbers:



Year 5

Year 5	• Subtract whole numbers with more than 4 digits. • Subtract numbers mentally with increasingly large numbers. • Subtract decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1 • Subtract fractions with the same denominator, and denominators that are multiples of the same number.
Progression of skills	**Key representations**
Subtract whole numbers with more than 4 digits Encourage children to estimate and use inverse operations to check answers to calculations.	I can exchange 1 … for 10 … 
Subtract using mental strategies Subtract 1s, 10s, 100s etc from any number. Use number bonds and related facts.	 48,650 – 300 = 48,650 – 30,000 = 48,650 – 30 = To subtract …, I can subtract … then add … 
Subtract decimals with up to 2 decimal places Progress from the same number of decimal places to a different number of decimal places and from no exchange to exchange.	
Complements to 1 Encourage children to make links with bonds to 10 and complements to 100 and 1,000 when finding a missing part or subtracting from 1	  10 – 4 = 6 100 – 44 = 56 1,000 – 444 = 556 1 – 0.4 = 0.6 1 – 0.44 = 0.56 1 – 0.444 = 0.556

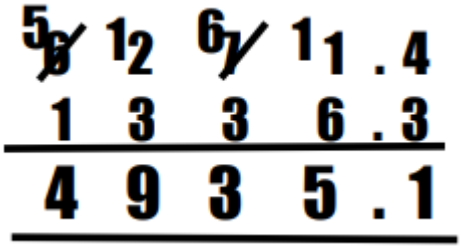
Year 6

Year 6	• Subtract larger numbers, using the formal written methods of columnar subtraction. • Use their knowledge of the order of operations to carry out calculations involving the 4 operations. • Calculate intervals across zero. • Subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions.
Progression of skills	**Key representations**
Subtract integers up to 10 million Encourage children to estimate and use inverse operations to check answers to calculations.	  
Subtract decimals with up to 3 decimal places Progress from the same number of decimal and whole number places to a different number of decimal and whole number places.	I do/do not need to make an exchange because …   
Order of operations Children learn the order of priority for operations in a calculation. Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.	… has greater priority than … , so the first part of the calculation I need to do is …  
Negative numbers Children subtract from positive and negative numbers and calculate intervals across 0	… minus … is equal to …    The difference between – 5 and –1 is 4  The difference between 5 and –5 is 10

Formal methods: Year 5 & 6

Subtract whole numbers with more than four-digits using column subtraction, (introduce addition of money and decimals using compact method)

Ensure when subtraction includes decimals that the decimal point **does not** move.

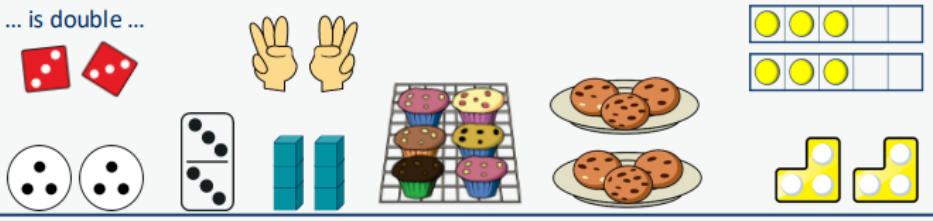
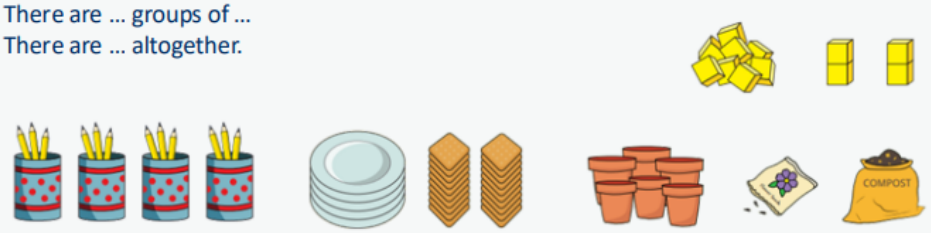


Multiplication

Year group	Skill
Nursery	• Continue with counting and subitising skills as a foundation for later work on equal groups. (see addition and subtraction sections)
Reception	• Double to 10 • Make equal groups
Year 1	• Count in 2s, 5s and 10s • Add equal groups • Make arrays • Make doubles
Year 2	• Link repeated addition and multiplication • Use arrays • Double • The 2 times-table • The 10 times-table • The 5 times-table • Missing numbers
Year 3	• The 3 times-table • The 4 times-table • The 8 times-table • Related facts • Multiply a 2-digit number by a 1-digit number - no exchange • Multiply a 2-digit number by a 1-digit number - with exchange • Scaling • Correspondence problems
Year 4	• Times-table facts to 12 × 12 • Multiply by 1 and 0 • Multiply 3 numbers • Factor pairs • Multiply by 10 and 100 • Related facts • Mental strategies • Multiply a 2 or 3-digit number by a 1-digit number • Scaling • Correspondence problems
Year 5	• Multiples and factors • Square and cube numbers • Multiply numbers up to 4 digits by a 1-digit number • Multiply numbers up to 4 digits by a 2-digit number • Multiply by 10, 100 and 1,000 • Mental strategies • Multiply fractions by a whole number • Multiply mixed numbers by a whole number • Find the whole
Year 6	• Multiply numbers up to 4 digits by a 2-digit number • Multiply by 10, 100 and 1,000 • Order of operations • Multiply decimals by integers • Multiply fractions by fractions • Find the whole • Calculations involving ratio

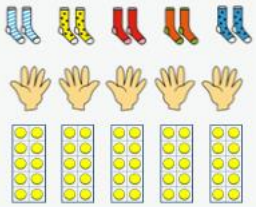
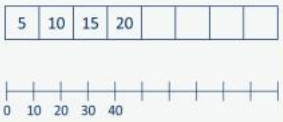
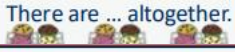
EYFS

PRACTICAL MATHS

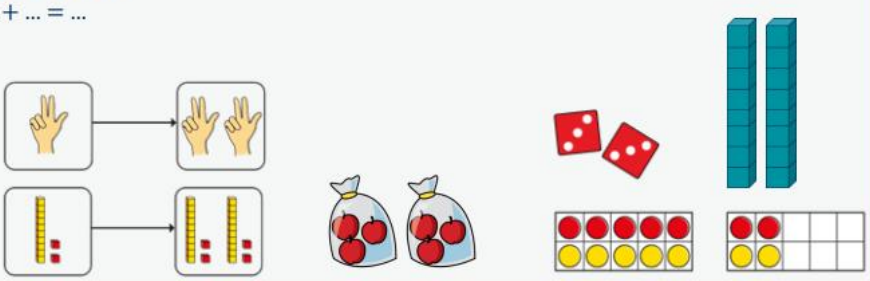
Reception	• Have a deep understanding of number to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts. • Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.
Progression of skills	**Key representations**
Double to 10 Prompt children to notice that double means twice as many and to notice that there are two equal groups.	Double ... is ... ... is double ... 
Make equal groups Provide opportunities to make equal groups when tidying up or during snack time. Encourage children to check that each group has the same amount.	There are ... groups of ... There are ... altogether. 

Year 1

<table>
<tr><td>Year 1</td><td colspan="3">• Count in multiples of twos, fives and tens.
• Solve one-step problems involving multiplication, using concrete objects, pictorial representations and arrays with the support of the teacher.</td></tr>
<tr><td>Progression of skills</td><td colspan="3">Key representations</td></tr>
<tr><td>Count in 2s, 5s and 10s

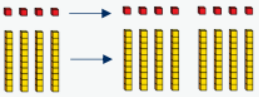
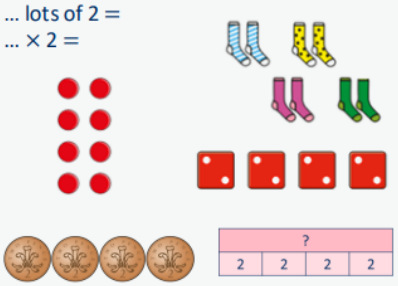
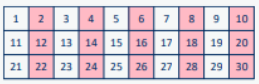
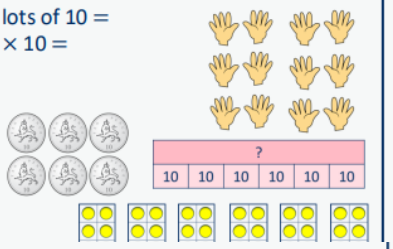
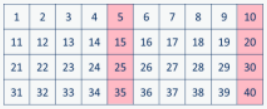
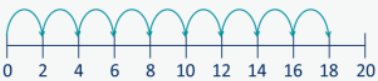
Begin by counting objects that naturally come in 2s, 5s and 10s, for example pairs of socks or fingers.</td><td>There are … equal groups of …
There are … altogether.
  </td><td>Continue to colour in …s
What do you notice?
  </td><td>Complete the number track/number line by counting in …s.
  </td></tr>
<tr><td>Add equal groups
(repeated addition)</td><td colspan="2">There are … groups of …
There are … altogether.
  </td><td>What is the same? What is different?
2 + 2 + 2 =</td></tr>
<tr><td>Make arrays

Children use their knowledge of adding equal groups to arrange objects in columns and rows.</td><td colspan="3">There are … rows of … There are … altogether.
There are … columns of … There are … altogether.
  </td></tr>
<tr><td>Make doubles

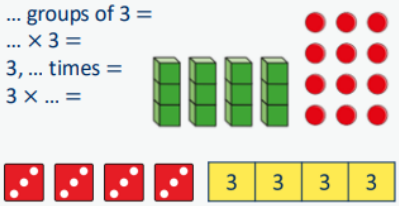
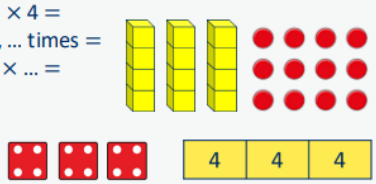
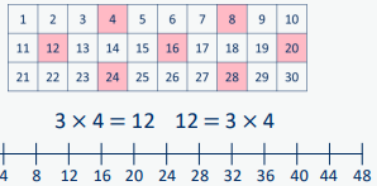
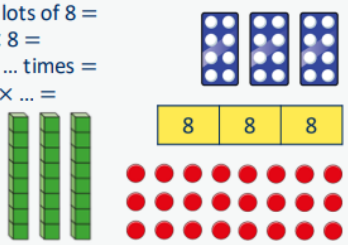
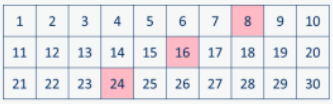
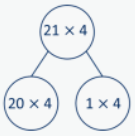
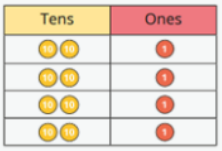
Children understand that doubles are two equal groups. Children may begin to explore doubles beyond 20 using base 10</td><td colspan="3">Double … is …
… + … = …
  </td></tr>
</table>

Use numicon to represent multiplication

Year 2

Year 2	• Recall and use multiplication facts for the 2, 5 and 10 multiplication tables. • Calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (×) and equals (=) signs. • Show that multiplication of two numbers can be done in any order (commutative).
Progression of skills	**Key representations**
Link repeated addition and multiplication Encourage children to make the link between repeated addition and multiplication.	There are … equal groups with … in each group. There are … altogether.  6 (3 + 3) 3 + 3 = 6 2 × 3 = 6  20 (5 + 5 + 5 + 5) 5 + 5 + 5 + 5 = 20 4 × 5 = 20
Use arrays Encourage children to see that multiplication is commutative.	There are … rows with … in each row. There are … columns with … in each column.  3 lots of 5 = 15 5 + 5 + 5 = 15 5 lots of 3 = 15 3 + 3 + 3 + 3 + 3 = 15 I can see … × … and … ×… 3 × 5 = 15 5 × 3 = 15 3 × 5 = 5 × 3
Double Encourage children to make links with related facts.	Double … is …  Double 4 = 4 + 4 Double 4 is 8 Double … is … so double … is …  Double 4 is 8 Double 40 is 80
The 2 times-table Encourage daily counting in multiples both forwards and back. Notice that all multiples of 2 are even numbers.	… lots of 2 = … × 2 =  ? (2 2 2 2) … times 2 is equal to …  1 × 2 = 2 2 = 1 × 2 2 × 2 = 4 4 = 2 × 2 3 × 2 = 6 6 = 3 × 2  0 2 4 6 8 10 12 14 16 18 20 22 24
The 10 times-table Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.	… lots of 10 = … × 10 =  ? (10 10 10 10 10) … times 10 is equal to …  1 × 10 = 10 10 = 1 × 10 2 × 10 = 20 20 = 2 × 10 3 × 10 = 30 30 = 3 × 10
The 5 times-table Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.	… lots of 5 = … × 5 =  ? (5 5 5 5 5) … times 5 is equal to …  1 × 5 = 5 5 = 1 × 5 2 × 5 = 10 10 = 2 × 5 3 × 5 = 15 15 = 3 × 5  0 5 10 15 20 25 30 35 40 45 50 55 60
Missing numbers Make links to known facts.	… is equal to … groups of … 18 socks, how many pairs?   0 2 4 6 8 10 12 14 16 18 20 … times … is equal to … □ × 2 = 18 18 = 2 × □

Year 3

Year 3	• Recall and use multiplication facts for the 3, 4 and 8 multiplication tables. • Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods. • Solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.
Progression of skills	**Key representations**
The 3 times-table Encourage daily counting in multiples both forwards and back.	… groups of 3 = … × 3 = 3, … times = 3 × … =  … times 3 is equal to …  4 × 3 = 12 12 = 4 × 3
The 4 times-table Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2 and 4 times-tables.	… groups of 4 = … × 4 = 4, … times = 4 × … =  … times 4 is equal to …  3 × 4 = 12 12 = 3 × 4
The 8 times-table Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2, 4 and 8 times-tables.	… lots of 8 = × 8 = 8, … times = 8 × … =  … times 8 is equal to …  3 × 8 = 24 24 = 3 × 8 
Related facts Use knowledge of multiplying by 10 to scale times-table facts.	… × … ones is equal to … ones so … × … tens is equal to … tens.  3 × 4 = 12 3 × 40 = 120
Multiply a 2-digit number by a 1-digit number - no exchange Children apply their understanding of partitioning to represent and solve calculations using the expanded method.	… tens multiplied by … is equal to … tens. …ones multiplied by … is equal to … ones.  30 × 2 = 60 2 × 2 = 4 32 × 2 = 64  

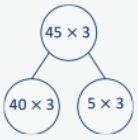
<table>
<tr>
<td>Multiply a 2-digit number by a 1-digit number - with exchange

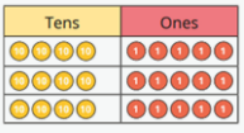
Children apply their understanding of partitioning to represent and solve calculations using the expanded method.</td>
<td colspan="2">... tens multiplied by ... is equal to ... tens.
... ones multiplied by ... is equal to ... ones.

$20 \times 4 = 80$
$4 \times 4 = 16$

$24 \times 4 = 96$


</td>
</tr>
<tr>
<td>Scaling

Children focus on multiplication as scaling (.... times the size) as opposed to repeated addition.</td>
<td>There are .... times as many ... as ...

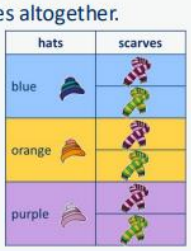
 

There are 3 times as many triangles as circles.</td>
<td>... is ... times the size of ...
... is ... times the length/height of ...


Miss Smith is twice the height of Jo.</td>
</tr>
<tr>
<td>Correspondence problems
(How many ways?)

Encourage children to work systematically to find all the different possible combinations.</td>
<td colspan="2">For every ... , there are ... possible ...
There are ... × ... possibilities altogether.

For every hat, there are two possible scarves.
$3 \times 2 = 6$

There are 6 possibilities altogether.</td>
</tr>
</table>

Show the written method alongside the manipulatives or pictorial representation

Formal method : Multiply two-digit by one-digit numbers.

Begin with multiplying a 2 digit by a 1 digit number:

$$\begin{array}{r} 3\ 2 \\ \times\quad 3 \\ \hline 9\ 6 \end{array}$$

Move onto adding an extra digit:

$$\begin{array}{r} 5\ 2 \\ \times\quad 4 \\ \hline 2\,0\,8 \end{array}$$

To extend pupils, move onto carrying. In multiplication, you must always carry at the top, never below.

$$\begin{array}{r} {\scriptstyle 5}\ 3\ 8 \\ \times\quad 7 \\ \hline 2\ 6\ 6 \end{array}$$

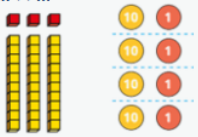
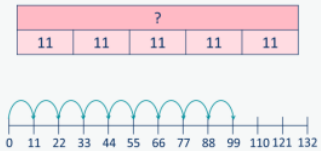
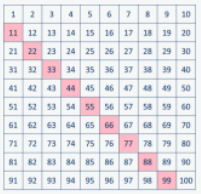
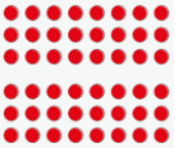
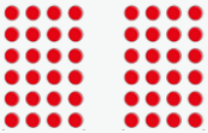
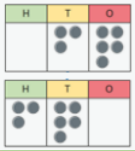
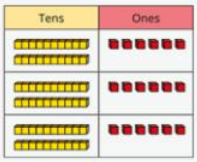
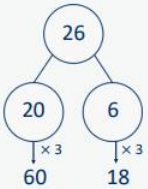
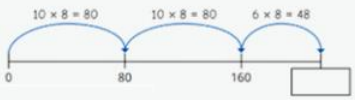
When carrying, carry above and cross out to show that you have added it on.

$3 \times 7 = 21$

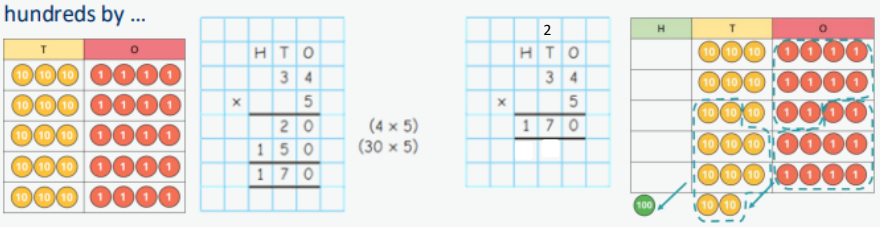
$21 + 5 = 26$ →

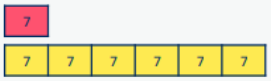
$$\begin{array}{r} \cancel{5}\ 3\ 8 \\ \times\quad 7 \\ \hline 2\ 6\ 6 \end{array}$$

Year 4

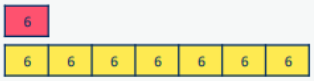
Year 4	• Recall multiplication facts for multiplication tables up to 12 × 12 • Use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three numbers. • Recognise and use factor pairs and commutativity in mental calculations. • Multiply two-digit and three-digit numbers by a one-digit number using formal written layout. • Solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.
Progression of skills	**Key representations**
Times-table facts to 12 × 12 Encourage daily counting in multiples both forwards and back. Encourage children to notice links between related times-tables.	... groups of ... = ... times ... is equal to ... ... × ... =   
Multiply by 1 and 0	Any number multiplied by 1 is equal to ... Any number multiplied by 0 is equal to ...  ... × ... = ... 1 × 1 = 1 1 × 0 = 0 2 × 1 = 2 2 × 0 = 0 3 × 1 = 3 3 × 0 = 0 4 × 1 = 4 4 × 0 = 0
Multiply 3 numbers Children use their understanding of commutativity to multiply more efficiently.	To work out ... × ... × ..., I can first calculate ... × ... and then multiply the answer by ...  4 × 2 × 3 = 8 × 3 = 24 2 × 3 × 4 = 6 × 4 = 24 3 × 4 × 2 = 12 × 2 = 24
Factor pairs Children explore equivalent calculations using different factors pairs.	12 = ... × ..., so ... × 12 = ... × ... × ...  8 × 6 = 8 × 3 × 2 8 × 6 = 24 × 2  6 × 8 = 6 × 4 × 2 6 × 8 = 24 × 2
Multiply by 10 and 100 Some children may over-generalise that multiplying by 10 or 100 always results in adding zeros. This will cause issues later when multiplying decimals.	When I multiply by 10, the digits move ... place value column to the left. ... is 10 times the size of ...  35 × 10 = 350 When I multiply by 100, the digits move ... place value columns to the left. ... is 100 times the size of ...  14 × 100 = 1,400
Related facts Use knowledge of multiplying by 10 and 100 to scale times-table facts.	... × ... ones is equal to ... ones so ... × ... tens is equal to ... tens and ... × ... hundreds is equal to ... hundreds.  3 × 7 = 21 7 × 3 = 21 3 × 70 = 210 7 × 30 = 210 3 × 700 = 2,100 7 × 300 = 2,100
Mental strategies Partition 2 or 3-digit numbers to multiply using informal methods.	... tens multiplied by ... is equal to ... tens. ...ones multiplied by ... is equal to ... ones.  3 × 26 = 60 + 18 = 78   26 × 8 = 80 + 80 + 48 = 208

<table>
<tr>
<td>Multiply a 2 or 3-digit number by a 1-digit number

The short multiplication method is introduced for the first time, initially in an expanded form.</td>
<td>To multiply a 2-digit number by … , I multiply the ones by … and the tens by …
To multiply a 3-digit number by … , I multiply the ones by … , the tens by … and the hundreds by …
 
</td>
</tr>
<tr>
<td>Scaling

Children focus on multiplication as scaling (… times the size).</td>
<td>… is … times the size of …
 

A computer mouse costs £7
A keyboard costs 6 times as much.

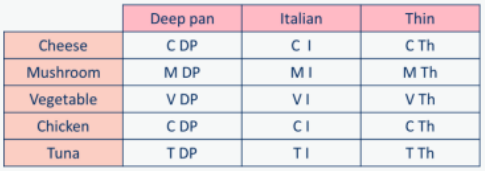
 

A red ribbon is 6 cm.
A yellow ribbon is 7 times as long.</td>
</tr>
<tr>
<td>Correspondence problems

Encourage children to use tables to show all the different possible combinations.</td>
<td>For every … , there are … possibilities.
There are … × … possibilities altogether.

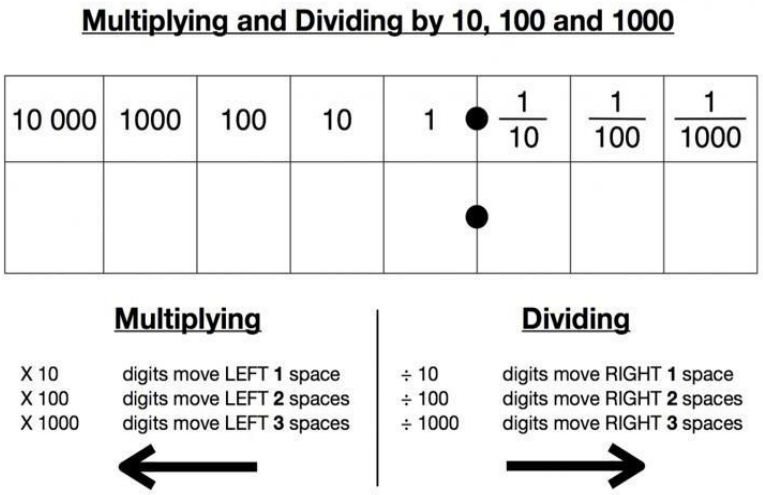
A pizza company offers a choice of 5 toppings and 3 bases.

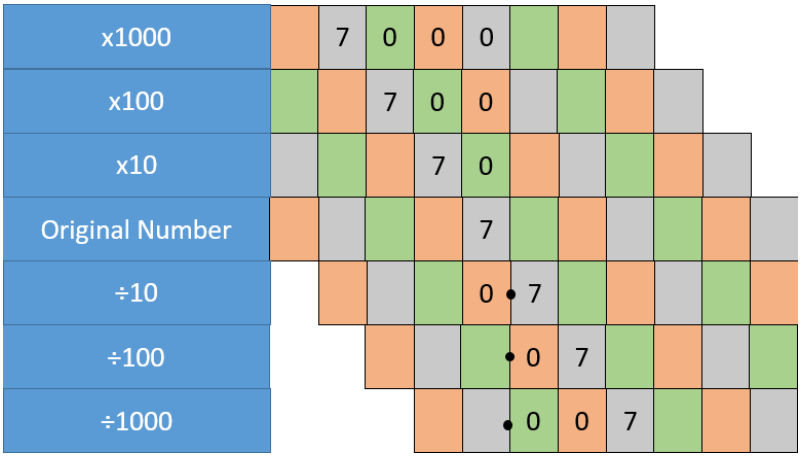
5 × 3 = 15

 
</td>
</tr>
</table>

- Multiply two-digit by one-digit, including decimals by 10, 100, 1000: Use place value sliders.

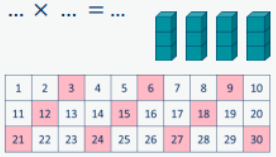
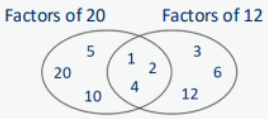
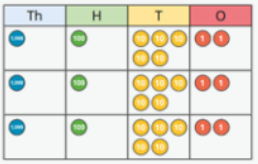
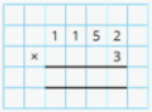
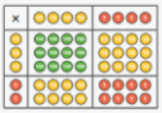
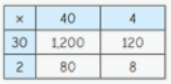
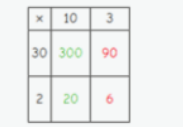
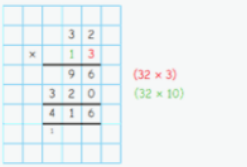
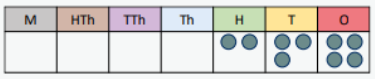
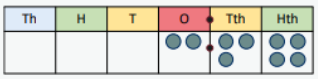
Children must be fully aware that the decimal point NEVER moves and the digits move instead.



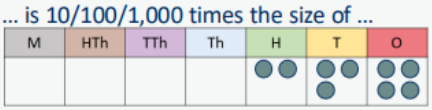
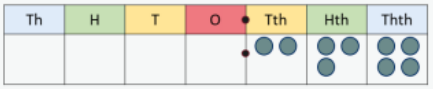
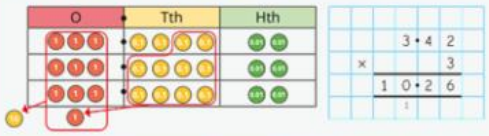
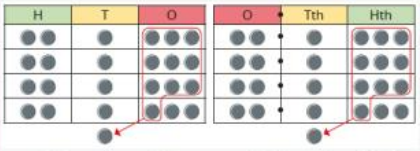


- By the end of Year 4, children must know all of their multiplication tables up to 12.

Year 5

Year 5	• Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers • Recognise and use square numbers and cube numbers, and the notation for squared (^{2}) and cubed (^{3}) • Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers. • Multiply numbers mentally drawing upon known facts. • Multiply whole numbers and those involving decimals by 10, 100 and 1000 • Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams.
Progression of skills	**Key representations**
Multiples and factors Encourage children to notice patterns and make links with known facts.	… is a multiple of … because … × … = …  … is a factor of … because … × … = …  1 × 8 2 × 4 1, 2, 4 and 8 are factors of 8 The common factors of … and … are … 
Square and cube numbers	… squared means … × …  1 × 1 = 1^2 = 1 2 × 2 = 2^2 = 4 3 × 3 = 3^2 = 9 4 × 4 = 4^2 = 16 … cubed means … × … × …  1 × 1 × 1 = 1^3 = 1 2 × 2 × 2 = 2^3 = 8 3 × 3 × 3 = 3^3 = 27
Multiply numbers up to 4 digits by a 1-digit number This builds on the short multiplication method introduced in Y4	To multiply a 4-digit number by … , I multiply the ones by … , the tens by … , the hundreds by … and the thousands by …  
Multiply numbers up to 4 digits by a 2-digit number Numbers are first partitioned using an area model then long multiplication is introduced for the first time.	I can partition … into … and …   32 × 44 = 1,200 + 80 + 120 + 8 32 × 44 = 1,408 First, I multiply by the … Then I multiply by the …  300 + 90 + 20 + 6 = 416 
Multiply by 10, 100 and 1,000 Some children may over-generalise that multiplying by a power of 10 always results in adding zeros. This will cause issues later when multiplying decimals.	To multiply by 10/100/1,000, I move all the digits … places to the left. … is 10/100/1,000 times the size of …  234 × 10 = 2,340 234 × 100 = 23,400 234 × 1,000 = 234,000  2.34 × 10 = 23.4 2.34 × 100 = 234 2.34 × 1,000 = 2,340
Mental strategies Children continue to use efficient mental strategies such as partitioning and knowledge of factor pairs and related facts to multiply.	The most efficient strategy to calculate … × … is … To calculate … × 12, I can do … × … × … For example: 121 × 12 I could calculate 100 × 12 plus 20 × 12 plus 1 × 12 I could calculate 121 × 10 plus 121 × 2 I could calculate 121 × 6 × 2 I could calculate 121 × 4 × 3

Year 6

Year 6	• Identify common factors and common multiples. • Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication. • Multiply numbers by 10, 100 and 1,000 • Multiply one-digit numbers with up to two decimal places by whole numbers. • Use their knowledge of the order of operations to carry out calculations involving the 4 operations. • Multiply simple pairs of proper fractions, writing the answer in its simplest form. • Solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts. • Solve problems involving the calculation of percentages.
Progression of skills	**Key representations**
Multiply numbers up to 4 digits by a 2-digit number	To multiply by a 2-digit number, first multiply by the ones, then multiply by the tens and then find the total. See below for formal method.
Multiply by 10, 100 and 1,000 Some children may over-generalise that multiplying by a power of 10 always results in adding zeros.	To multiply by 10/100/1,000, I move all the digits ... places to the left. ... is 10/100/1,000 times the size of ...   $234 \times 10 = 2{,}340$ $234 \times 100 = 23{,}400$ $234 \times 1{,}000 = 234{,}000$ $0.234 \times 10 = 2.34$ $0.234 \times 100 = 23.4$ $0.234 \times 1{,}000 = 234$
Order of operations Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.	... has greater priority than ..., so the first part of the calculation I need to do is ...   $(3 + 4) \times 2 = 14$  $3 + 4^2 = 19$  $3 + 4 \times 2 = 11$
Multiply decimals by integers This is the first time children multiply decimals by numbers other than 10, 100 or 1,000 Encourage them to make links with known facts and whole number multiplication.	I know that ... × ... = ..., so I also know that ... × ... = ...  $6 \times 2 = 12$ $6 \times 0.2 = 1.2$	I need to exchange 10 ... for 1 ...   $213 \times 4 = 852$ $2.13 \times 4 = 8.52$

<table>
<tr><th>Progression of skills</th><th colspan="2">Key representations</th></tr>
<tr><td>Calculate percentages

Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.</td><td>There are … lots of … % in 100%
To find … %, I need to divide by …

<table><tr><td colspan="4">100%</td></tr><tr><td colspan="2">50%</td><td colspan="2">50%</td></tr><tr><td>25%</td><td>25%</td><td>25%</td><td>25%</td></tr></table>
50% of … = …÷ 2
25% of … = …÷ 4</td><td>… % is made up of … %, and … %

<table><tr><td colspan="10">100%</td></tr><tr><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td></tr></table>
To find 30%, I can find 10% and then multiply it by 3
To find 23%, I can use 10% × 2 and 1% × 3
To find 99%, I can find 1%, then subtract from 100%</td></tr>
<tr><td>Calculations involving ratio

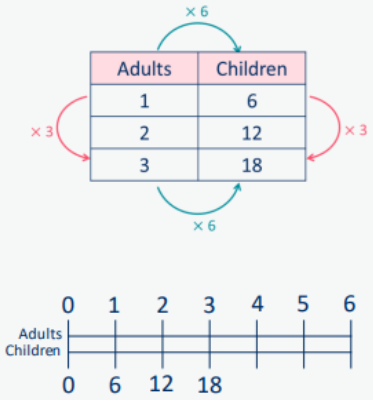
Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent.
Double number lines and ratio tables help children to see both horizontal and vertical multiplicative relationships.</td><td colspan="2">For every … , there are …

For every 1 adult on a school trip, there are 6 children.

adults

children

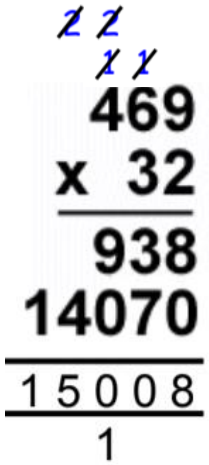
The ratio of adults to children is 1 : 6

 
</td></tr>
</table>

Formal methods Year 5 & 6:

Multiplying numbers up to four-digit by 1 and two-digit numbers using long multiplication

1) 9 x 2 = 18, place the 8 carry the 1 which is a ten
2) 60 x 2 = 120 + carried 1 ten = 130 (once carried cross it out, place the 3 carry the 1 hundred)
3) 400 x 2 = 800 + carried 1 hundred = 900
4) Cross out the 2 as it has now been used
5) Place a 0 to show you are multiplying by 10 (place value holder)
6) 9 x 30 = 270, place the 7 carry the 2 hundred
7) 60 x 30 = 1,800 + carried 2 hundred = 2,000 (once carried cross it out , place the 0 carry the 2)
8) 400 x 30 = 12,000 + carried 2,000 = 14,000 (place both numbers as there is nothing left to multiply by)
9) Now add the two rows using column addition and carry below



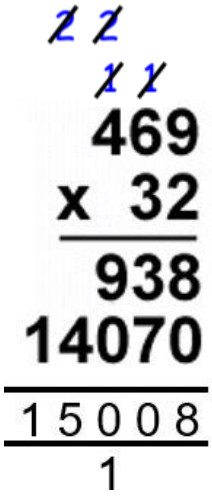
Always remember your **place value holder**, you need to a place a zero to hold the place of the ten. Therefore, if you are multiplying by hundreds, you need to place two place value holders, as there are two places of value within a hundred.

Multiplying decimals

Apply the same method for multiplying decimals, but remove the decimal point until the calculation is complete. Once the calculation is complete, put the decimal point back. You can identify where the decimal point needs to go by counting the decimal places in the sum.

E.g. **46.9** x **3.2** =

Two decimal places = **150.08**

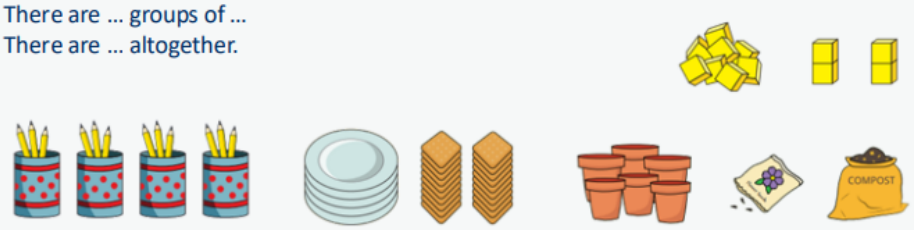


Division

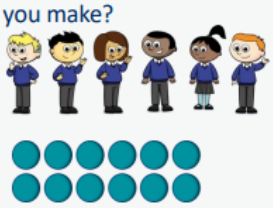
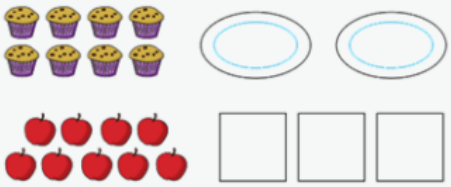
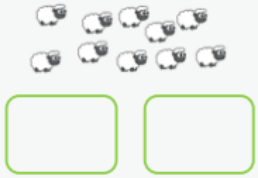
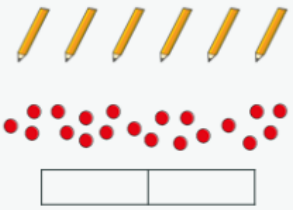
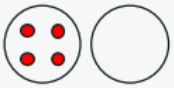
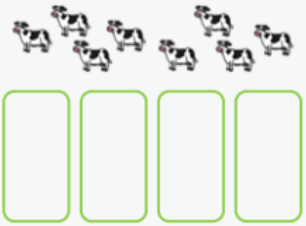
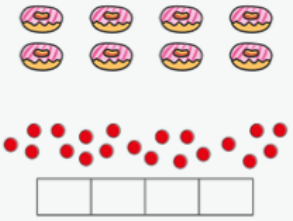
Year group	Skill
Nursery	• Continue with counting and subitising skills as a foundation for later work on equal groups. (see addition and subtraction sections)
Reception	• Sharing • Grouping
Year 1	• Make equal groups – grouping • Make equal groups – sharing • Find a half • Find a quarter
Year 2	• Divide by 2 • Divide by 10 • Divide by 5 • Missing numbers • Unit fractions • Non-unit fractions
Year 3	• Divide by 3 • Divide by 4 • Divide by 8 • Related facts • Divide a 2-digit number by a 1-digit number - no exchange • Divide a 2-digit number by a 1-digit number - with remainders • Unit fractions of a set of objects • Non-unit fractions of a set of objects
Year 4	• Division facts to 12 × 12 • Divide a number by 1 and itself • Related facts • Divide a 2 or 3-digit number by a 1-digit number • Divide by 10 and 100
Year 5	• Mental strategies • Divide numbers up to 4 digits by a 1-digit number • Divide by 10, 100 and 1,000 • Fraction of an amount
Year 6	• Short division • Mental strategies • Long division • Order of operations • Divide by 10, 100 and 1,000 • Divide decimals by integers • Decimal and fraction equivalents • Divide a fraction by an integer • Fraction of an amount • Calculate percentages • Calculations involving ratio

EYFS

PRACTICAL MATHS

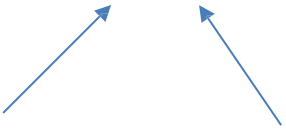
Reception	• Have a deep understanding of number to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts. • Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.
Progression of skills	**Key representations**
Sharing Provide practical activities such as sharing items during snack time. Encourage children to check whether items have been shared fairly (equally).	There are … altogether. They are shared equally between … groups. 
Grouping Provide opportunities to make equal groups when tidying up or during snack time. Encourage children to check that each group has the same amount.	There are … groups of … There are … altogether. 

Year 1

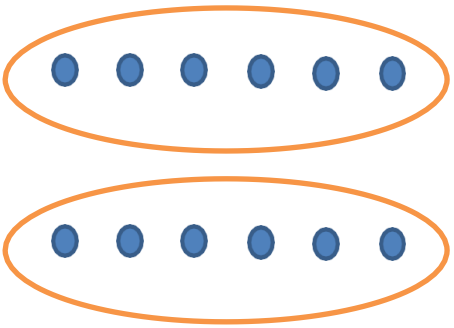
Year 1	• Solve simple one-step problems involving division, using concrete objects, pictorial representations and arrays with the support of the teacher. • Recognise, find and name a half as one of two equal parts of a quantity. • Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity.		
Progression of skills	**Key representations**		
Make equal groups - grouping Encourage children to physically move objects into equal groups. They can also circle equal groups when using pictures.	There are ... altogether. How many groups of ... can you make? 	Circle groups of 2 There are ... groups of 2 	Take ... cubes. Make equal groups.  There are ... groups of ...
Make equal groups – sharing Encourage children to check that the objects have been shared fairly and each group is the same.	... have been shared equally between... There are ... on/in each ... 	Take ... cubes. Share them between ...  12 shared between ... is ...	
Find a half Start with practical opportunities to share a quantity into 2 groups. Progress to circling half of the objects in a picture and then to finding the whole from a given half.	To find half, I need to share into 2 equal groups.  There are ... in each group.	Half of ... is ... 	If ... is half, what is the whole?  4 is half of ...
Find a quarter Start with practical opportunities to share a quantity into 4 groups. Progress to using pictures or bar models to find a quarter and then to finding the whole from a given quarter.	To find a quarter, I need to share into 4 equal groups.  There are ... in each group.	A quarter of ... is ... 	If ... is one quarter, what is the whole?  3 is one quarter of ...

Find a half: Halving and sharing using manipulatives

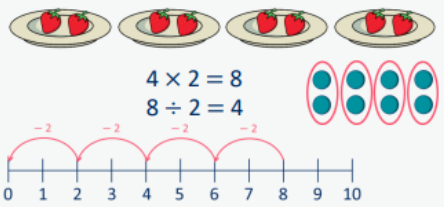
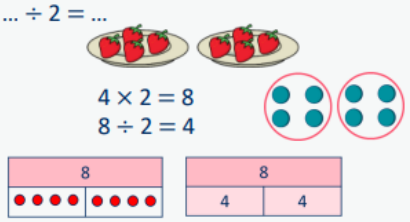
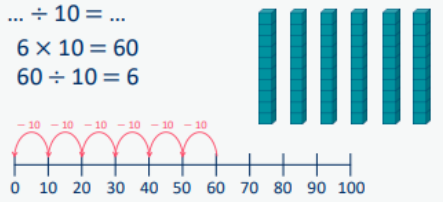
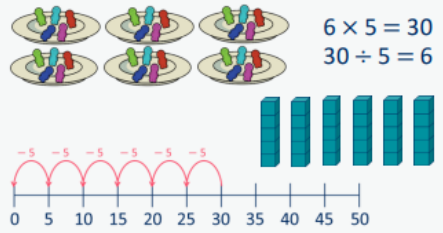
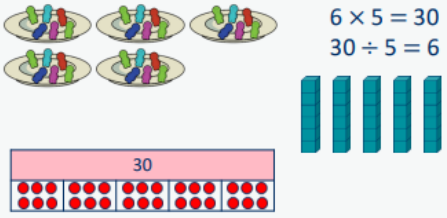
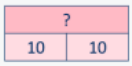
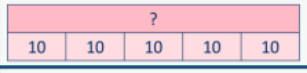
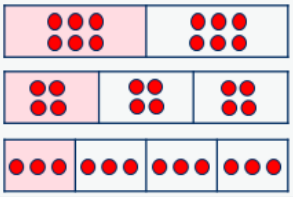
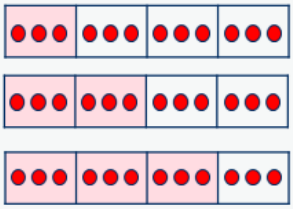
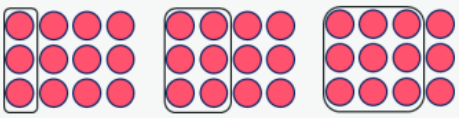
Division as arrays 12 ÷ 2 =



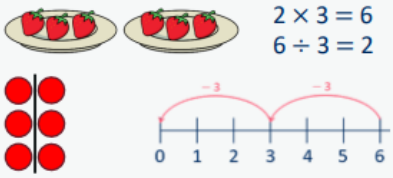
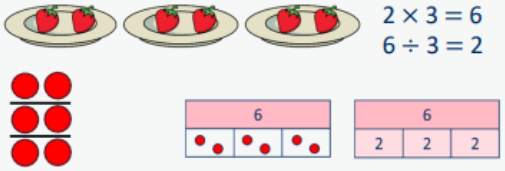
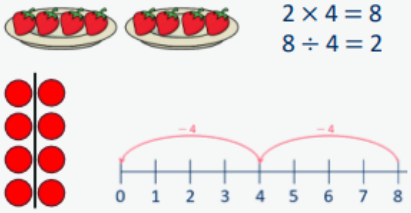
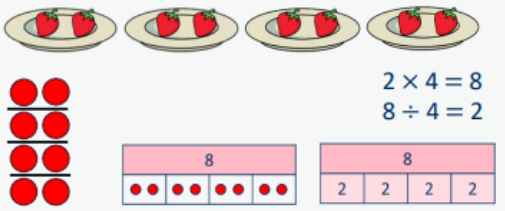
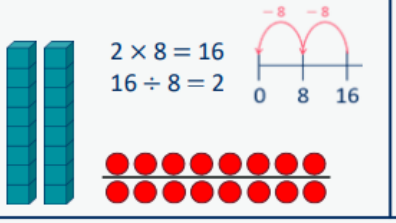
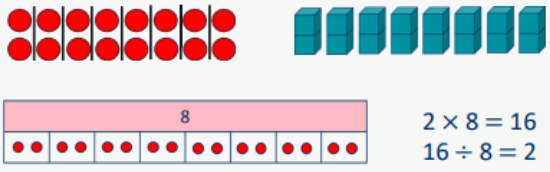
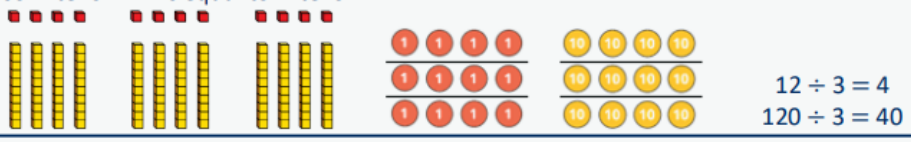
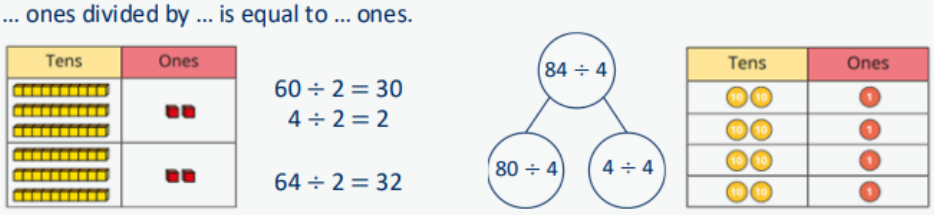
Number of objects **Number of rows**

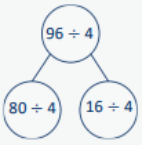
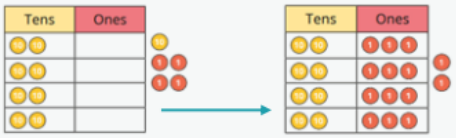
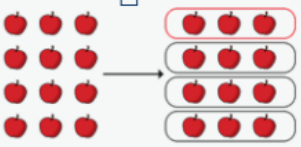
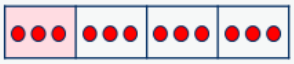
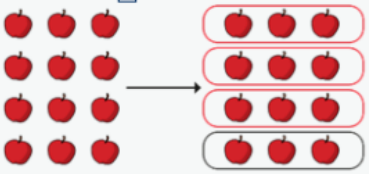
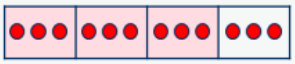


Year 2

Year 2	• Recall and use division facts for the 2, 5 and 10 multiplication tables. • Calculate mathematical statements for division within the multiplication tables and write them using the division (÷) and equals (=) signs. • Recognise, find, name and write fractions $\frac{1}{3}, \frac{1}{4}, \frac{2}{4}$ and $\frac{3}{4}$ of a quantity.	
Progression of skills	**Key representations**	
Divide by 2 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts and halving.	There are … equal groups of 2 … ÷ 2 = …  	… shared equally between 2 is … Half of … is … … ÷ 2 = … 
Divide by 10 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are … equal groups of 10 … ÷ 10 = …  	… shared equally between 10 is … … ÷ 10 = … 
Divide by 5 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are … equal groups of 5 … ÷ 5 = …  	… shared equally between 5 is … … ÷ 5 = … 
Missing numbers Bar models are useful to show the link between multiplication and division.	… divided by 2/5/10 is equal to …  □ ÷ 2 = 10  □ ÷ 5 = 10	
Unit fractions In Y2 the focus is on finding $\frac{1}{2}, \frac{1}{4}$ and $\frac{1}{3}$ Bar models are useful to show the link between division and finding a fraction.	The objects have been shared fairly into … groups. $\frac{1}{\square}$ of … is … 	There are … equal parts. There is … part circled. $\frac{1}{\square}$ is circled. 
Non-unit fractions In Y2 the focus is on finding $\frac{2}{4}$ and $\frac{3}{4}$ Prompt children to notice that $\frac{2}{4}$ is equivalent to $\frac{1}{2}$	The objects have been shared fairly into … groups. $\frac{\square}{\square}$ of … is … 	There are … equal parts. There are … parts circled. $\frac{\square}{\square}$ is circled. 

Year 3

Year 3	• Recall and use division facts for the 3, 4 and 8 multiplication tables. • Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods. • Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators.
Progression of skills	**Key representations**
Divide by 3 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... groups of 3 in ... ... ÷ 3 =  ... has been shared equally into 3 equal groups. ... ÷ 3 = 
Divide by 4 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... groups of 4 in ... ... ÷ 4 =  ... has been shared equally into 4 equal groups. ... ÷ 4 = 
Divide by 8 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... groups of 8 in ... ... ÷ 8 =  ... has been shared equally into 8 equal groups. ... ÷ 8 = 
Related facts Link to known times-table facts.	... ÷ ... is equal to ..., so ... tens ÷ ... is equal to ... tens. 
Divide a 2-digit number by a 1-digit number - no exchange Partition into tens and ones to divide and then recombine.	... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones. 

Divide a 2-digit number by a 1-digit number - with remainders Encourage children to partition numbers flexibly to help them to divide more efficiently.	… tens divided by … is equal to … tens. … ones divided by … is equal to … ones.   80 ÷ 4 = 20 16 ÷ 4 = 4 96 ÷ 4 = 24	There are … groups of … There are … remaining. 31 ÷ 4 = 7 r3  94 ÷ 4 = 23 r2 
Unit fractions of a set of objects Bar models are useful to show the link between division and fractions, for example, dividing by 3 and finding a third.	The whole is divided into … equal parts. Each part is $\frac{1}{\square}$ of the whole.  $\frac{1}{4}$ of 12 apples is 3 apples.	One … of … is … $\frac{1}{4}$ of 12 is 3  $\frac{1}{3}$ of 36 is 12 
Non-unit fractions of a set of objects Bar models are a useful representation and show the links with division and multiplication.	The whole is divided into … equal parts. Each part is $\frac{1}{\square}$ of the whole.  $\frac{3}{4}$ of 12 apples is 9 apples.	$\frac{1}{\square}$ of … is …, so $\frac{\square}{\square}$ of … is … $\frac{3}{4}$ of 12 is 9  $\frac{2}{3}$ of 36 is 24 

Formal method: Show formal methods alongside concrete and pictorial examples.

Divide two-digit numbers by one-digit. Teachers must ensure pupils are aware of place value in order to find the correct answer.

$$2\overline{)84}$$

$$\begin{array}{r} 4 \\ 2\overline{)84} \end{array}$$ Do the 8 first, 8÷2=4

$$\begin{array}{r} 42 \\ 2\overline{)84} \end{array}$$ Then do the 4, 4÷2=2

1) How many groups of 2 can you make with 8?
   8 ÷ 2 = 4
2) Place the 4 above the 8 in the tens column.
3) How many 2s can you make with 4?
   4 ÷ 2 = 2
4) Place the 2 above the 4 in the ones column.
5) Children to read the answer using an understanding of place value as 42.

Once children are able to divide whole numbers equally, move onto numbers with a remainder.

$4\overline{)64}$

1) How many groups of 4s in 6?

   6 ÷ 4 = 1 r 2

$$\begin{array}{r} 1 \\ 4\overline{)6^{2}4} \end{array}$$

2) Place the 1 above the 1 and carry the 2 across to the 4

   (Making the number 24)

3) How many groups of 4s in 24?

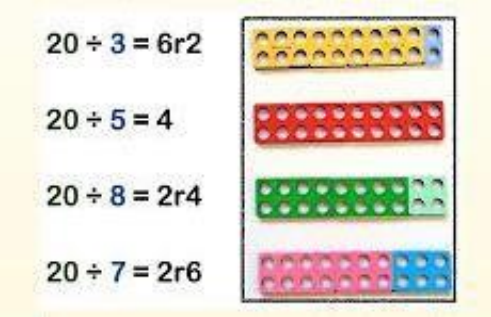
   24 ÷ 4 = 6

$$\begin{array}{r} 16 \\ 4\overline{)6^{2}4} \end{array}$$

4) Place the 6 above the 24, the answer becomes 16

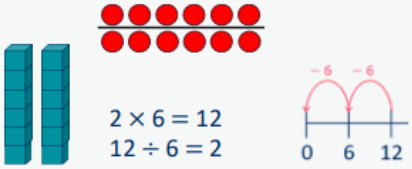
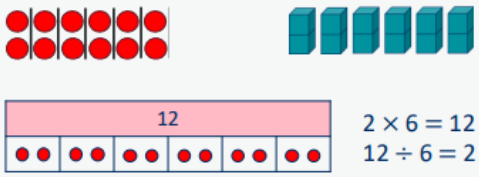
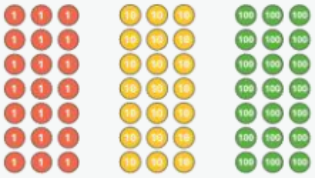
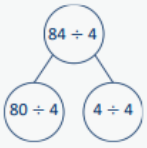
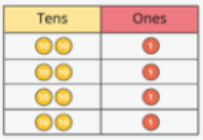
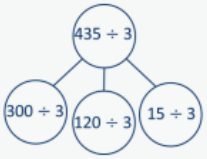
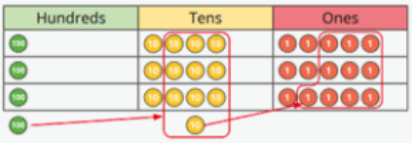
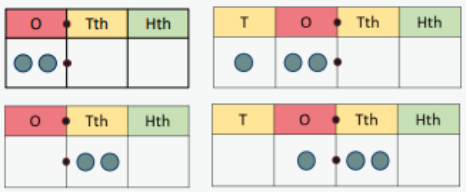
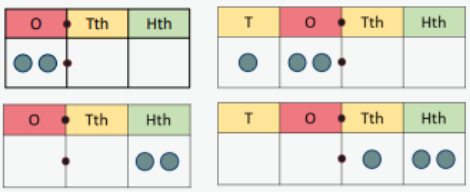
   64 ÷ 4 = 16

Numicon can also be used to help children understand the concept of reminders:



Year 4

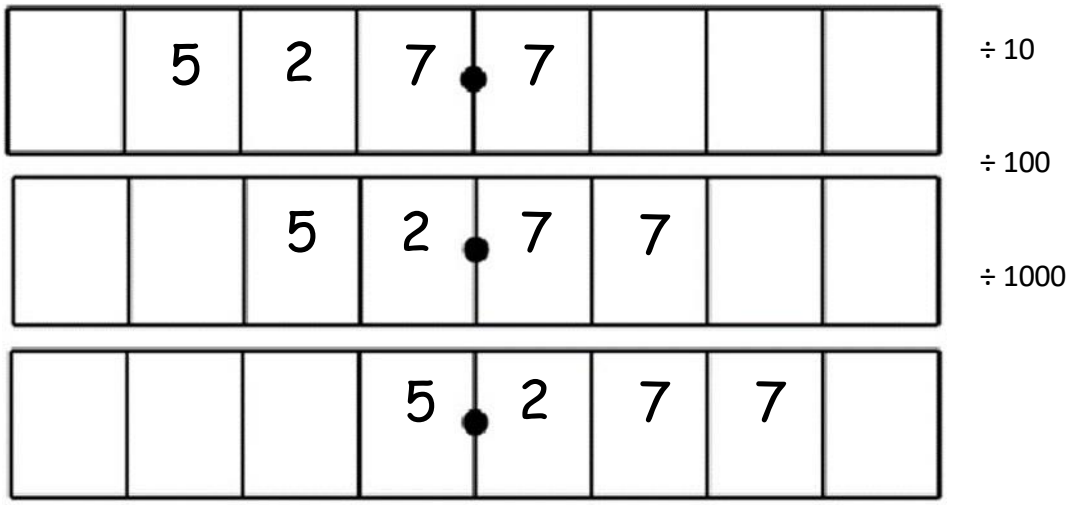
Year 4	• Recall division facts for multiplication tables up to 12 × 12 • Use place value, known and derived facts to divide mentally, including: dividing by 1 • Find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths.

Progression of skills	Key representations	
Division facts to 12 × 12 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are … groups of … in … … ÷ … =  	… has been shared equally into … equal groups. … ÷ … = 
Divide a number by 1 and itself Children may try to divide a number by zero and it should be highlighted that this is not possible.	When I divide a number by 1, the number remains the same. 5 shared between 1 is 5  There are **5** groups of 1 in 5 	When I divide a number by itself, the answer is 1 5 shared between 5 is 1  There is **1** group of 5 in 5 
Related facts Link to known times-table facts.	… ÷ … is equal to … so … tens ÷ … is equal to … tens and … hundreds ÷ … is equal to … hundreds.  21 ÷ 7 = 3 210 ÷ 7 = 30 2,100 ÷ 7 = 300 21 ÷ 3 = 7 210 ÷ 3 = 70 2,100 ÷ 3 = 700	
Divide a 2 or 3-digit number by a 1-digit number Progress from divisions with no exchange, to divisions with exchange and then divisions with remainders.	I can partition … into … tens and … ones.  80 ÷ 4 = 20 4 ÷ 4 = 1 84 ÷ 4 = 21  	I cannot share the hundreds/tens equally, so I need to exchange 1 … for 10 …  300 ÷ 3 = 100 120 ÷ 3 = 40 15 ÷ 3 = 5 435 ÷ 3 = 145 
Divide by 10 and 100 Encourage children to notice that dividing by 100 is the same as dividing by 10 twice.	When I divide by 10, the digits move 1 place value column to the right. … is one-tenth the size of …  2 ÷ 10 = 0.2 12 ÷ 10 = 1.2	When I divide by 100, the digits move 2 place value columns to the right. … is one-hundredth the size of …  2 ÷ 100 = 0.02 12 ÷ 100 = 0.12

- Divide two-digit by one-digit, including decimals by 10, 100, 1000.

5277 ÷ 10 = 527.7
5277 ÷ 100 = 52.77
5277 ÷ 1000 = 5.277

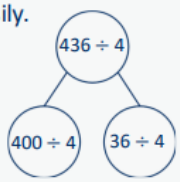
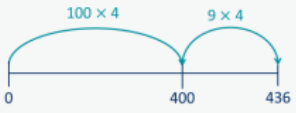
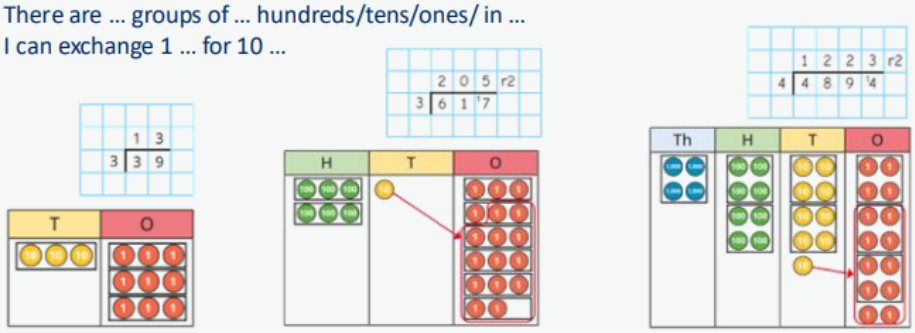
Just like multiplication, ensure the decimal point never moves and the digits move instead.



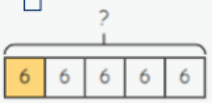
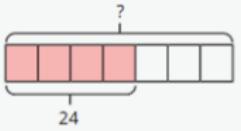
Formal method: See year 3

Year 5

Year 5	• Divide numbers mentally drawing upon known facts. • Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context. • Divide whole numbers and those involving decimals by 10, 100 and 1,000

Progression of skills	Key representations		
Mental strategies	I can partition ... into ... and ... to help me to divide more easily. 	I can show groups of ... on a number line. 	To divide by ..., I can divide by ... and then divide the result by ... 436 ÷ 4 = 436 ÷ 2 ÷ 2 436 ÷ 2 = 218 218 ÷ 2 = 109
Divide numbers up to 4 digits by a 1-digit number	There are ... groups of ... hundreds/tens/ones/ in ... I can exchange 1 ... for 10 ... 		

Divide by 10, 100 and 1,000 Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.	To divide by 10/100/1,000, I move all the digits ... places to the right. ... is one-tenth/one-hundredth/one-thousandth the size of ... 	120 ÷ 10 = 12 120 ÷ 100 = 1.2 120 ÷ 1,000 = 0.12

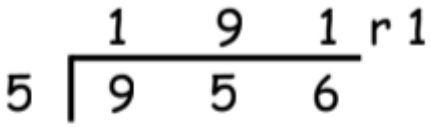
Fraction of an amount Bar models support children to understand that to find a fraction of an amount, we divide by the denominator and multiply by the numerator.	To find $\frac{\square}{\square}$ of ... , I need to divide by ... and multiply by ...  $\frac{1}{5}$ of 20 = $\frac{3}{5}$ of 20 = $\frac{1}{4}$ of 84 = $\frac{3}{4}$ of 84 =	If $\frac{1}{\square}$ is ... , then the whole is ... × ...  $\frac{1}{5}$ of ___ = 6  $\frac{4}{7}$ of ___ = 24

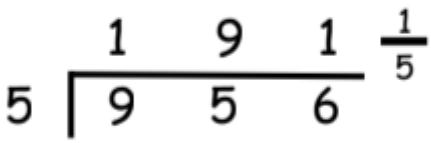
Formal method:

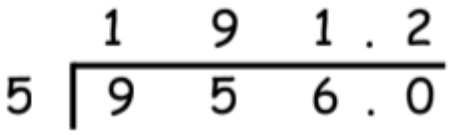
Divide up to four-digits by one-digit using short division, interpret remainders as fractions and decimals.

Pupils to divide using the same method as Year 3 and 4, but moving onto bigger numbers and interpreting remainders in different ways.

956 ÷ 5 = **191 r 1** OR **191.2** OR **191 ⅕**







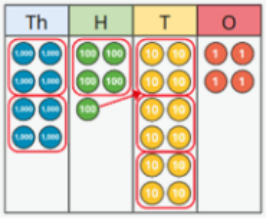
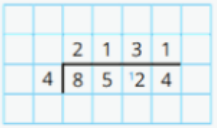
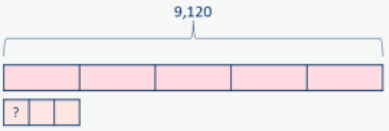
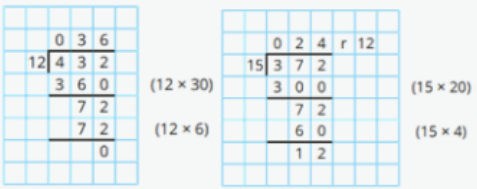
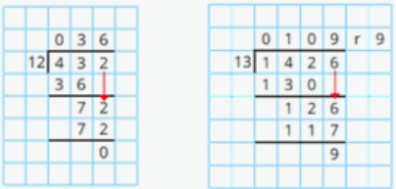
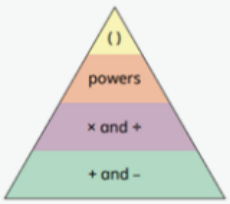
As you can see, there are three different ways to interpret the remainders, making each answer slightly different.

Pupils must be able to interpret simple remainders in the relevant context, depending on the problem they are solving.

Children should use this knowledge to answer division word problems such as:

- How many boxes do you need? (Round answer down to nearest whole number)
- How many boxes can you fill? (Round answer up to next whole number

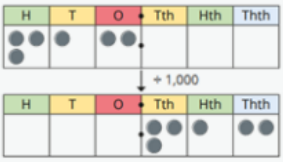
Year 6

Year 6	• Perform mental calculations, including with mixed operations and large numbers. • Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context. • Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context. • Divide numbers by 10, 100 and 1,000 giving answers up to three decimal places. • Use written division methods in cases where the answer has up to two decimal places. • Associate a fraction with division and calculate decimal fraction equivalents. • Divide proper fractions by whole numbers [for example, $\frac{1}{3} \div 2 = \frac{1}{6}$] • Solve problems involving the calculation of percentages.
Progression of skills	**Key representations**
Short division Encourage children to interpret remainders in context, for example knowing that "4 remainder 1" could mean 4 complete boxes with 1 left over so 5 boxes will be needed.	There are … groups of … hundreds/tens/ones/ in … I can exchange 1 … for 10 …  
Mental strategies Include partitioning and number line strategies outlined in Y5 as well as division using factors.	To divide by … , I can first divide by … and then divide the answer by … 240 ÷ 60 = 240 ÷ 10 ÷ 6  480 ÷ 24 = 480 ÷ 4 ÷ 6  9,120 ÷ 15 = 9,120 ÷ 5 ÷ 3 
Long division The long division method is introduced for the first time. Two alternative methods are shown.	Method 1  Method 2 
Order of operations Calculations in brackets should be done first, then powers. Multiplication and division should be performed before addition and subtraction.	… has greater priority than …, so the first part of the calculation I need to do is …   $(6 + 4) \div 2 = 5$  $6 + 4 \div 2 = 8$

Divide by 10, 100 and 1,000

Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.

To divide by … , I move the digits … places to the right.



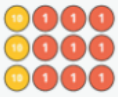
$312 \div 10 = 31.2$
$312 \div 100 = 3.12$
$312 \div 1{,}000 = 0.312$

$906 \div 10 = 90.6$
$906 \div 100 = 9.06$
$906 \div 1{,}000 = 0.906$

Divide decimals by integers

This is the first time children divide decimals by numbers other than 10, 100 or 1,000

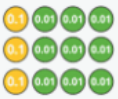
I know that … ÷ … = …,
so I also know that … ÷ … = …



$39 \div 3 = 13$

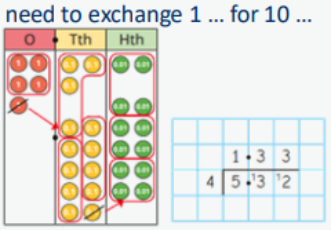


$3.9 \div 3 = 1.3$



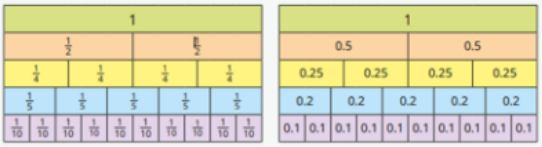
$0.39 \div 3 = 0.13$

I need to exchange 1 … for 10 …



Decimal and fraction equivalents

The fraction … is equivalent to the decimal …



$\frac{1}{5} = 0.2$ $\frac{2}{5} = 0.4$ $\frac{3}{5} = 0.6$

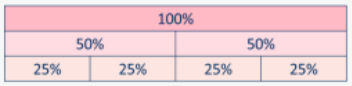
$\frac{\square}{\square}$ is equal to $\frac{\square}{100}$

$\frac{3}{4} \times 25 = \frac{75}{100} = 0.75$ (× 25)

Calculate percentages

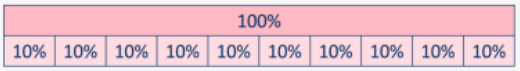
Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.

There are … lots of … % in 100%
To find … %, I need to divide by …



50% of … = …÷ 2
25% of … = …÷ 4

… % is made up of … %, and … %



To find 30%, I can find 10% and then multiply it by 3
To find 23%, I can use 10% × 2 and 1% × 3
To find 99%, I can find 1%, then subtract from 100%

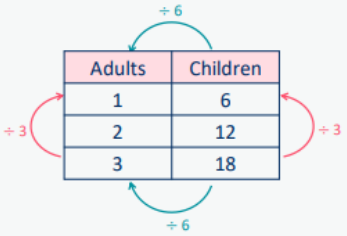
Calculations involving ratio

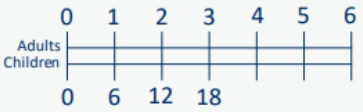
Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent.
Double number lines and ratio tables help children to see both horizontal and vertical multiplicative relationships.

For every … , there are …

For every 6 children on a school trip, there is 1 adult.







The ratio of children to adults is 6 : 1

By the time pupils reach year 6, they should be able to divide four-digit numbers by one- digit and interpret remainders in different ways (as shown above). The focus for year 6 is to divide numbers with up to four-digits by two-digits. See example B.

B =

		0	1	8	2
2	1)	3	$^{3}8$	$^{17}2$	$^{4}2$
	21		126		
	42		147		
	63		168		
	84		189		
	105		210		

Tip: Encourage children to estimate their times tables, rather than writing out entire lists of times tables.

E.g.: 1 x 21 = 21

$$\begin{array}{r|l} & \;\;0\;\;1\;\;8\;\;2 \\ \hline 21 & 3\;{}^{3}8\;{}^{17}2\;{}^{4}2 \end{array}$$

5 x 21 = 105
10 x 21 = 210

8 x 21 = 168
172 - 168 = 4

Pupils can estimate based on these key times tables what the answers could be.

1) First begin to write out your 21 times table. Advise children to use estimation if this takes too long.
2) Next look at how many 21s in 3? The answer is 0, therefore you have to carry the 3.
3) The 3 is carried over to the 8, making 38. How many 21s in 38? The answer is 1, place the 1 above the 38.
4) You now need to work out the remainder. 38 – 21 = 17
5) This stage requires you to carry 17 over to the 2, making 172.
6) How many 21s in 172? 21 x 8 = 168, therefore you place 8 above 172.
7) Now work out the remainder, 172 – 168 = 4, therefore you have to carry the 4 over to the 2, making 42.
8) Finally, how many 21s in 42? The answer is 2 and there are no remainders, which means the 2 needs to go above the 42, making the answer 182.
9) If the answer doesn't divide exactly, you may interpret the remainders in the same way as shown in Year 5 division.

Multiplication and Division

This should be memorised by individuals from 1-12 times tables with their corresponding division facts. Including multiplications and divisions with differing place values:

60 x 7 = 420   0.9 x 4 = 3.6   30 x 40 = 1200
180 ÷ 6 = 30   240 ÷ 80 =3   3.2 ÷ 0.8 = 4

Doubling and Halving

Doubling

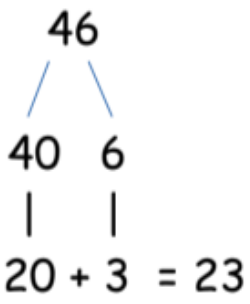
When doubling any number pupils need to be aware that they are multiplying by two but work it out by means of repeated addition.

$$34 \times 2 = 68$$
$$34 + 34 = 68$$

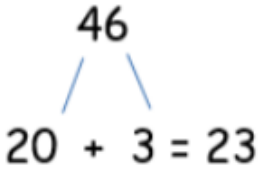
Halving

Whenever a problem presents as ÷2, children are to halve it using this method to reinforce that divide by 2 is the same as halving. When halving children to use their knowledge of partitioning. a) is the initial teaching and b) and c) show progression.

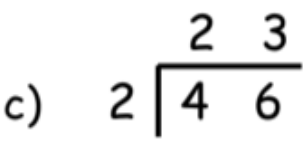
a)



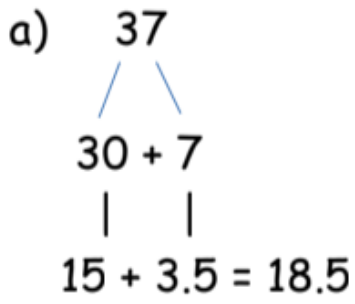
b)



c)



a)



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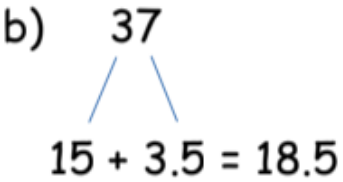
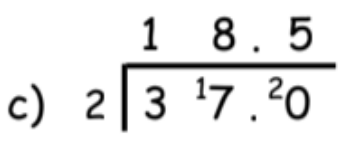


c)

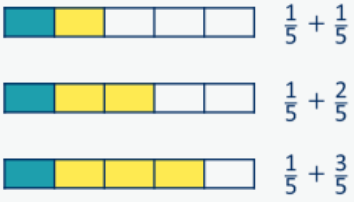
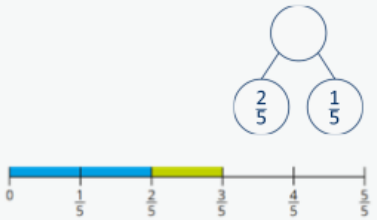
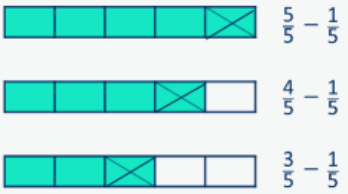
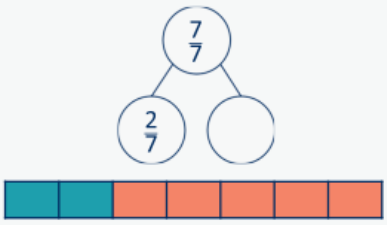


Fractions

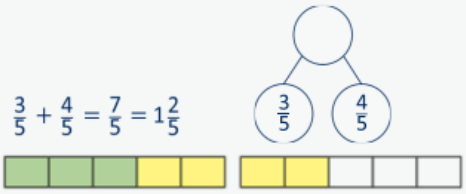
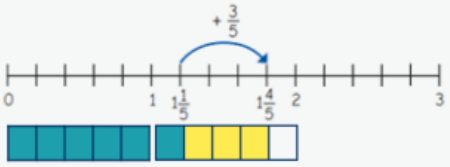
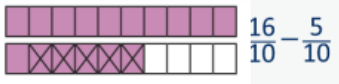
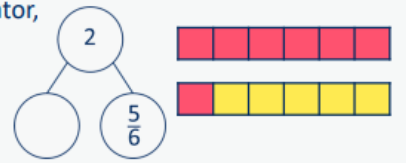
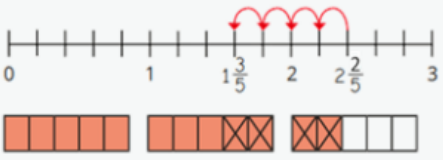
This covers fractions and the four operations – not simplifying and finding equivalents.

Addition and Subtraction of Fractions

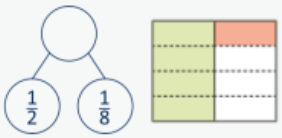
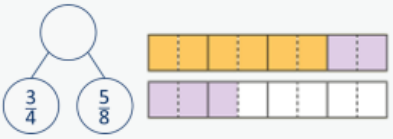
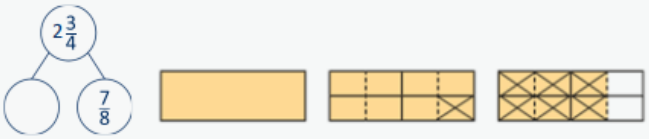
Year 3

Add fractions with the same denominator within 1 whole Make links with known facts.	When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths  
Subtract fractions with the same denominator within 1 whole Make links with known facts.	When subtracting fractions with the same denominator, I only subtract the numerator. ... fifths − ... fifths = ... fifths  

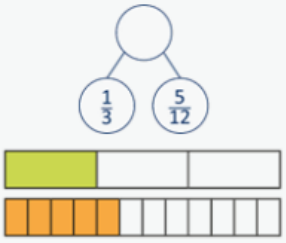
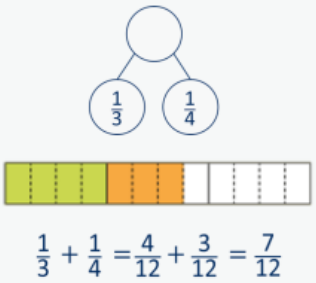
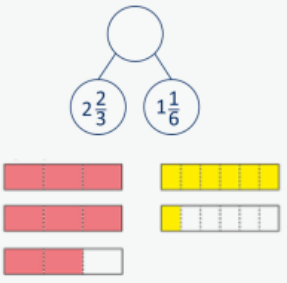
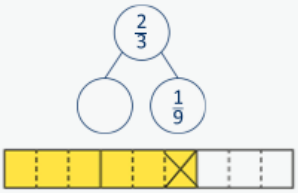
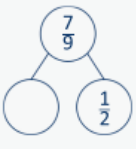
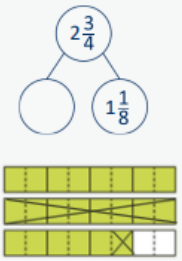
Year 4

Add fractions and mixed numbers with the same denominator beyond 1 whole	When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths  
Subtract fractions and mixed numbers with the same denominator Include subtracting fractions from wholes.	When subtracting fractions with the same denominator, I only subtract the numerator. ... tenths − ... tenths = ... tenths    

Year 5

Add fractions with denominators that are a multiple of one another Encourage children to convert fractions to the same denominator before adding. Progress from adding fractions within 1 whole to adding fractions beyond 1 whole.	The denominator has been multiplied by …, so the numerator needs to be multiplied by… for the fractions to be equivalent.  $\frac{1}{2} + \frac{1}{8} = \frac{4}{8} + \frac{1}{8} = \frac{5}{8}$  $\frac{1}{4} + \frac{3}{8} = \frac{2}{8} + \frac{3}{8} = \frac{5}{8}$  $\frac{3}{4} + \frac{5}{8} = \frac{6}{8} + \frac{5}{8} = \frac{11}{8} = 1\frac{3}{8}$
Subtract fractions with denominators that are a multiple of one another Convert fractions to the same denominator before subtracting. Progress from subtracting fractions within 1 whole to subtracting from a mixed number.	The denominator has been multiplied by …, so the numerator needs to be multiplied by… for the fractions to be equivalent.  $\frac{1}{3} - \frac{1}{15} = \frac{5}{15} - \frac{1}{15} = \frac{4}{15}$  $\frac{2}{3} - \frac{2}{9} = \frac{6}{9} - \frac{2}{9} = \frac{4}{9}$ 

Year 6

Add fractions Convert fractions to the same denominator before adding. Progress from fractions where one denominator is a multiple of the other, to any fractions and then to mixed numbers.	The denominator has been multiplied by …, so the numerator needs to be multiplied by … 	The lowest common multiple of … and … is …  $\frac{1}{3} + \frac{1}{4} = \frac{4}{12} + \frac{3}{12} = \frac{7}{12}$	…is made up of … wholes and … 
Subtract fractions Convert fractions to the same denominator before subtracting. Progress from fractions where one denominator is a multiple of the other, to any fractions and then subtracting from a mixed number.	The denominator has been multiplied by …, so the numerator needs to be multiplied by…  $\frac{2}{3} - \frac{1}{9} = \frac{6}{9} - \frac{1}{9} = \frac{5}{9}$	The lowest common multiple of … and … is …  $\frac{7}{9} - \frac{1}{2} = \frac{14}{18} - \frac{9}{18} = \frac{5}{18}$	… is made up of … wholes and …  $2\frac{3}{4} - 1\frac{1}{8} = 1\frac{5}{8}$

Formal methods: Year 5 & 6

- Add and subtract fractions where the denominators are multiples of the same number

Q. $\frac{1}{2} + \frac{3}{8} =$

The denominators need to be the same so the half needs to become four eighths.

$\frac{1}{2} \xrightarrow{\times 4} \frac{\mathbf{4}}{\mathbf{8}}$ (×4 on both numerator and denominator)

$\frac{\mathbf{4}}{\mathbf{8}} + \frac{3}{8} = \frac{7}{8}$

Q. $\frac{1}{2} + \frac{1}{3} =$

The denominators need to be the same. 6 is the lowest common multiple of 3 and 2 and therefore should be used as the denominator.

$\frac{1}{2} \xrightarrow{\times 3} \frac{\mathbf{3}}{\mathbf{6}}$ (×3 on both numerator and denominator)

$\frac{1}{3} \xrightarrow{\times 2} \frac{\mathbf{2}}{\mathbf{6}}$ (×2 on both numerator and denominator)

$\frac{3}{6} + \frac{2}{6} = \frac{5}{6}$

Multiplying and Dividing Fractions Multiplying fractions

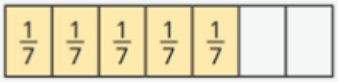
Year 5

Multiply fractions by a whole number

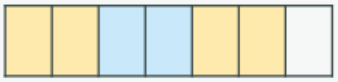
Make links with repeated addition.

E.g. $\frac{1}{5} \times 4 = \frac{1}{5} + \frac{1}{5} + \frac{1}{5} + \frac{1}{5}$

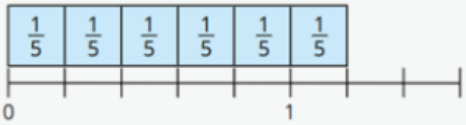
To multiply a fraction by an integer, I multiply the numerator by the integer and the denominator remains the same.



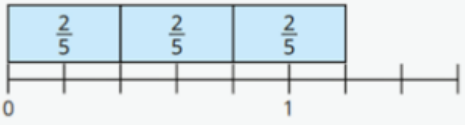
$\frac{1}{7} \times 5 = \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} = \frac{5}{7}$



$\frac{2}{7} \times 3 = \frac{2}{7} + \frac{2}{7} + \frac{2}{7} = \frac{6}{7}$



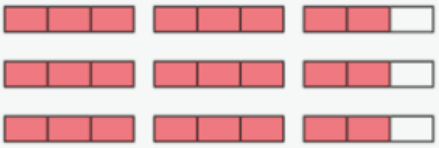
$\frac{1}{5} \times 6 = \frac{6}{5} = 1\frac{1}{5}$



$\frac{2}{5} \times 3 = \frac{6}{5} = 1\frac{1}{5}$

Multiply mixed numbers by a whole number

I can partition $\square\frac{\square}{\square}$ into $\square$ and $\frac{\square}{\square}$



$2\frac{2}{3} \times 3$

$2 \times 3 = 6$ $\quad \frac{2}{3} \times 3 = \frac{6}{3} = 2$

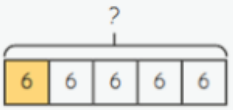
$2\frac{2}{3} \times 3 = 6 + 2 = 8$

Find the whole

Children multiply to find the whole from a given part.

If $\frac{1}{\square}$ is … , then the whole is … × …

$\frac{1}{5}$ of $\_\_ = 6$

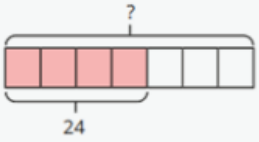


$5 \times 6 = 30$

$\frac{1}{5}$ of **30** $= 6$

If $\frac{\square}{\square}$ is … , then $\frac{1}{\square}$ is … and the whole is … × …

$\frac{4}{7}$ of $\_\_ = 24$



$\frac{1}{7} = 24 \div 4 = 6$

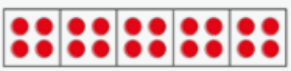
$7 \times 6 = 42$

$\frac{4}{7}$ of **42** $= 24$

Fraction of an amount

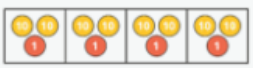
Bar models support children to understand that to find a fraction of an amount, we divide by the denominator and multiply by the numerator.

To find $\frac{\square}{\square}$ of … , I need to divide by … and multiply by …



$\frac{1}{5}$ of $20 =$

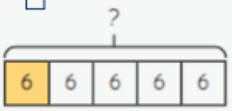
$\frac{3}{5}$ of $20 =$



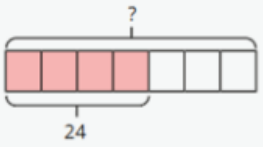
$\frac{1}{4}$ of $84 =$

$\frac{3}{4}$ of $84 =$

If $\frac{1}{\square}$ is … , then the whole is … × …



$\frac{1}{5}$ of $\_\_ = 6$

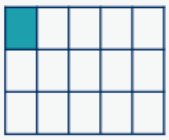
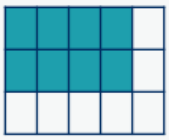
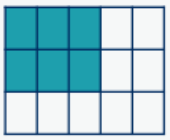


$\frac{4}{7}$ of $\_\_ = 24$

Year 6

<table>
<tr>
<td>Multiply fractions by fractions

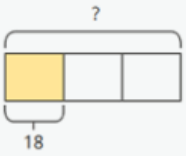
Encourage children to give answers in their simplest form.</td>
<td colspan="3">When multiplying a pair of fractions, I need to multiply the numerator and multiply the denominator.

$\frac{1}{3} \times \frac{1}{5} = \frac{1}{15}$ $\frac{2}{3} \times \frac{4}{5} = \frac{8}{15}$ $\frac{2}{3} \times \frac{3}{5} = \frac{6}{15} = \frac{2}{5}$</td>
</tr>
<tr>
<td>Find the whole

Children multiply to find the whole from a given part.</td>
<td colspan="2">If $\frac{1}{\square}$ is … , then the whole is … × …

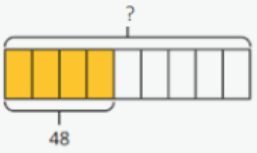
$\frac{1}{3}$ of ___ = 18

18 × 3 = 54

$\frac{1}{3}$ of 54 = 18</td>
<td>If $\frac{\square}{\square}$ is … , then $\frac{1}{\square}$ is … and the whole is … × …

$\frac{4}{9}$ of ___ = 48

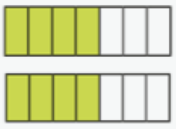
 

$\frac{1}{9} = 48 \div 4 = 12$

9 × 12 = 108

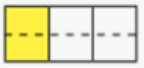
$\frac{4}{9}$ of 108 = 48</td>
</tr>
<tr>
<td>Divide a fraction by an integer

This is the first time children divide fractions by an integer.</td>
<td>… ones divided by 2 is … ones so … sevenths divided by 2 is … sevenths.

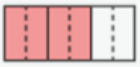
 

$\frac{4}{7} \div 4 = \frac{1}{7}$

$\frac{4}{7} \div 2 = \frac{2}{7}$</td>
<td>I am dividing by … , so I can split each part into … equal parts.

$\frac{1}{3} \div 2 = \frac{1}{6}$</td>
<td>… is equivalent to … so … ÷ … = … ÷ …

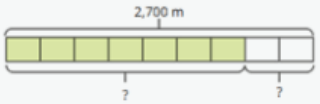
$\frac{2}{3} = \frac{4}{6}$

so $\frac{2}{3} \div 4 = \frac{4}{6} \div 4 = \frac{1}{6}$</td>
</tr>
<tr>
<td>Fraction of an amount

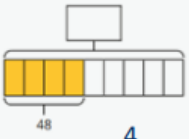
Children divide and multiply to find fractions of an amount. Bar models can still be used to support understanding where needed.</td>
<td>To find $\frac{1}{\square}$ I divide by …

$\frac{1}{2}$ of 36 = 36 ÷ 2

$\frac{1}{12}$ of 36 = 36 ÷ 12</td>
<td>If $\frac{1}{\square}$ is equal to …, then $\frac{\square}{\square}$ are equal to …

$\frac{7}{9}$ of 2,700 = $\frac{1}{9}$ of 2,700 × 7</td>
<td>If $\frac{\square}{\square}$ is equal to …, then the whole is equal to …

$\frac{4}{9}$ of ___ = 48</td>
</tr>
</table>

Multiplying fractions

1. Simplify the fractions if not in lowest terms.
2. Multiply the numerators of the fractions to get the new numerator.
3. Multiply the denominators of the fractions to get the new denominator.

Multiply the numerators

$$\frac{2}{5} \times \frac{3}{4} = \frac{6}{\quad}$$

Multiply the denominators

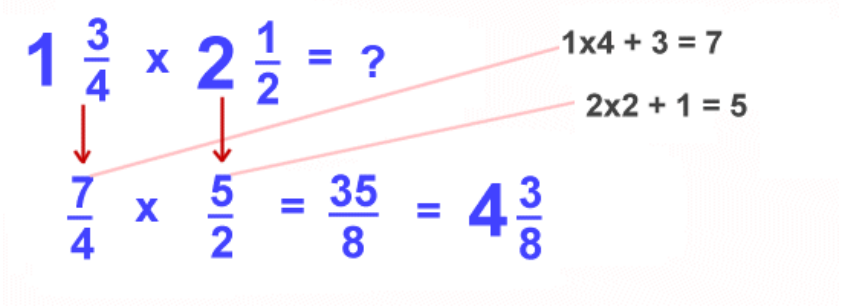
$$\frac{2}{5} \times \frac{3}{4} = \frac{6}{20}$$

Reduce the fraction if necessary

$$\frac{6}{20} = \frac{3}{10}$$

Multiplying Mixed Numbers

When multiplying mixed numbers you need to change the mixed number into an improper fraction before you multiply.



For example, if the number is $2\frac{1}{3}$, you will need to change this to $\frac{7}{3}$ before you multiply. You may also need to change the answer back to a mixed number when you have finished multiplying.

In this example $1\frac{3}{4}$ has been changed to the fraction $\frac{7}{4}$ and $2\frac{1}{2}$ to the fraction $\frac{5}{2}$. The multiplied answer was then converted back to a mixed number at the end.

Dividing Fractions

Keep, change, flip

1. Keep the first fraction.

2: Change the division sign to a multiplication sign.

3. Flip the second fraction, so the denominator becomes the numerator and the numerator becomes the denominator.

4: Solve the problem using multiplication skills, then simplify. You may need to convert from an improper fraction to a mixed number.

Converting improper fractions:

First you need to divide the numerator by the denominator. Your mixed number becomes the amount of times your total can equally divide into your denominator and your remainder becomes your numerator. Don't forget to simplify if and when possible.

$$\frac{7}{3} \div \frac{2}{8} = \frac{7}{3} \times \frac{8}{2}$$

Keep *Change* *Flip*

$$\frac{7}{3} \times \frac{8}{2} = \frac{56}{6}$$

$$\frac{56}{6} = 56 \div 6 = 9 \text{ r } 3$$

$$9 \text{ r } 3 = 9\frac{3}{6} = 9\frac{1}{2}$$